

ASTR 511

Galactic Astronomy

Lecture 11

Gravitational Potentials

Notes about scheduling

- Reminder: March 2 class is now **Friday March 3 at 10 AM**
 - Prospective grads!
- HW 3 nominally due tomorrow
- Final Project, Part 1 due tomorrow
 - Talks: March 7 and 9 (7-10min, you pick the style)
 - Term Paper due March 14
- Planning to release HW 4 (final assignment) tomorrow!

Gravitational Potential

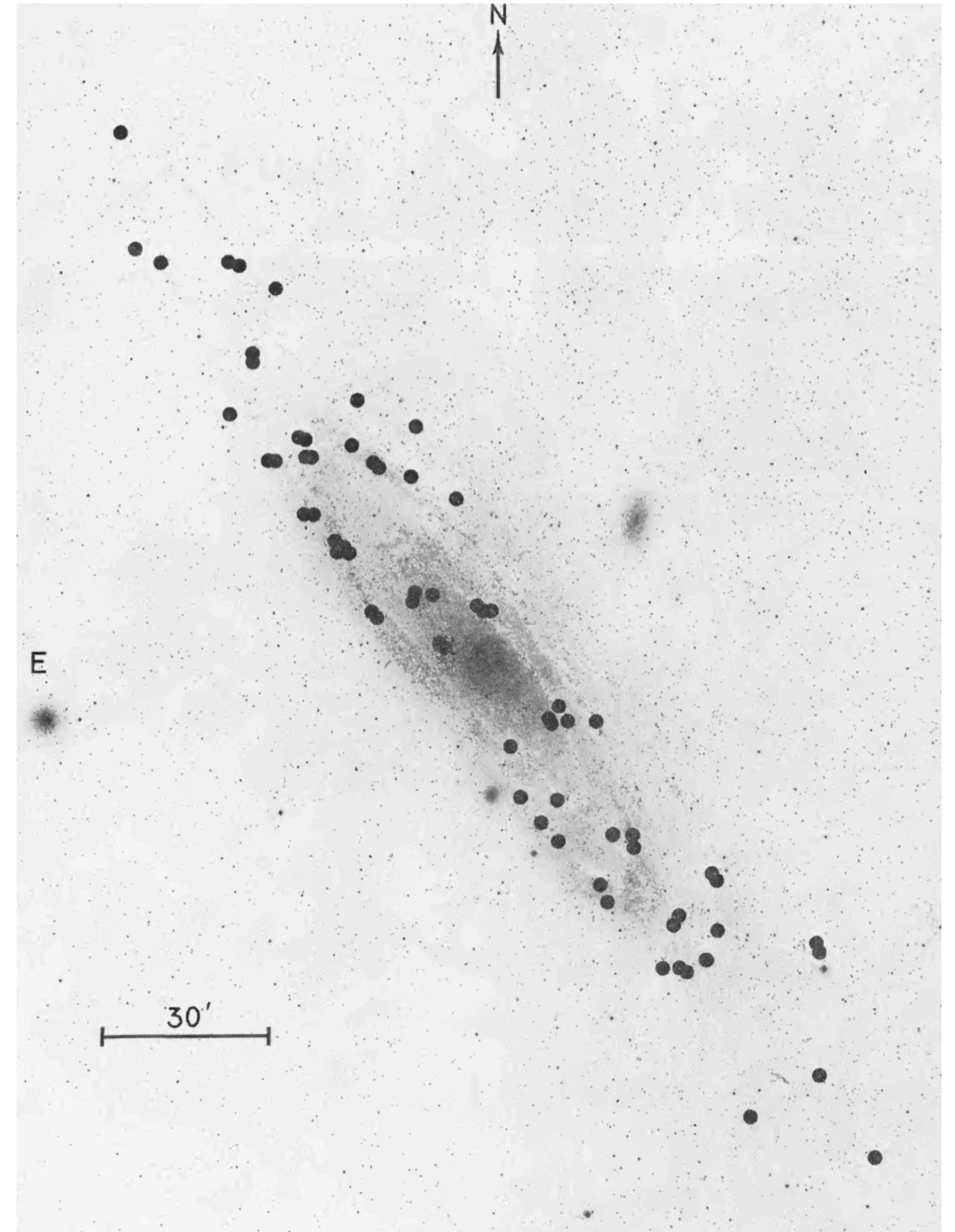
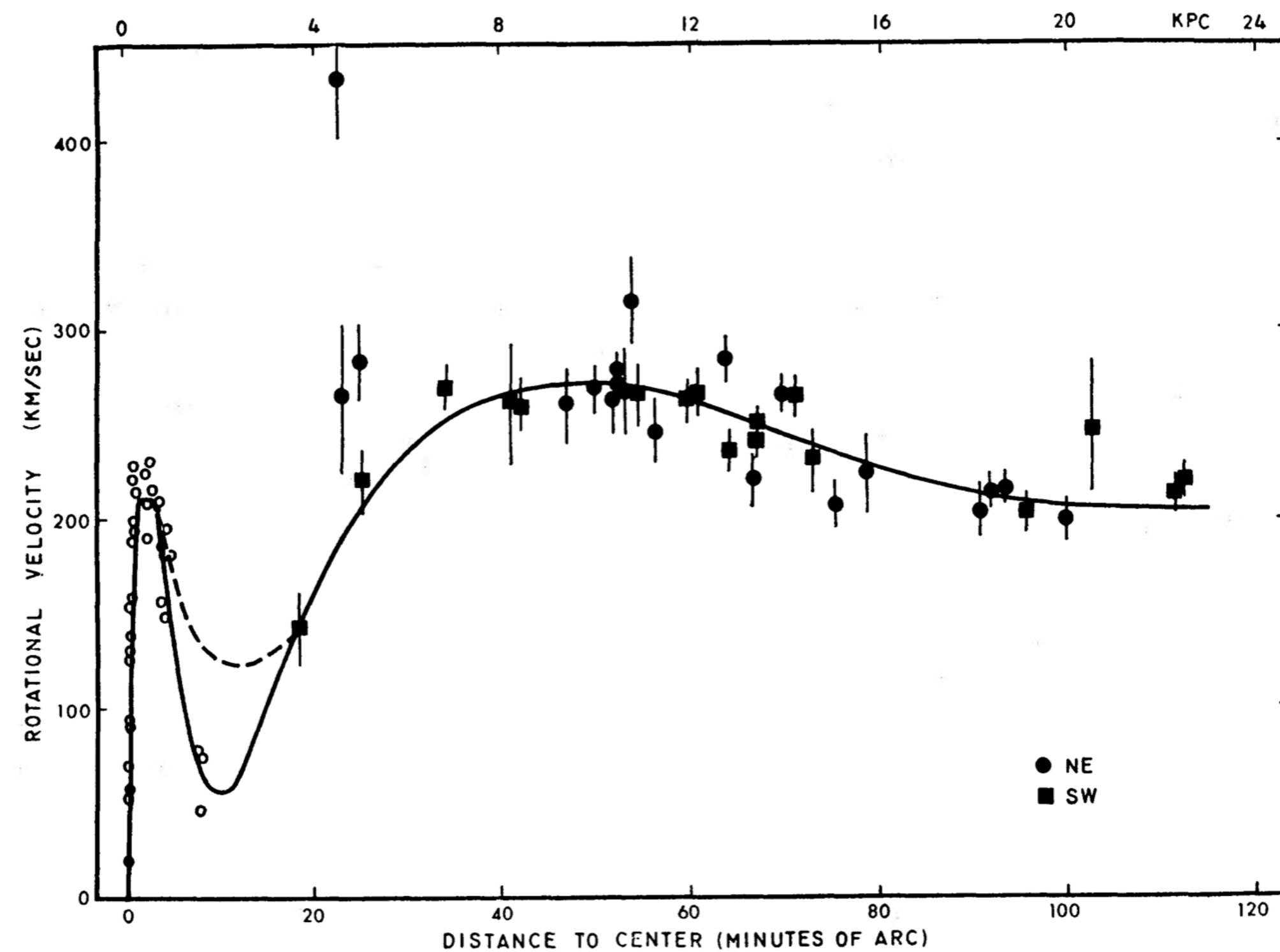
- $\Phi(r) = -\frac{GM}{r}$ (grav. potential energy radially from a point mass)
- MWY is *not* a point mass, so Φ depends on *enclosed* mass
 - Recall: Sag A* and nuclear cluster are not very massive, compared to disk(s), halo, etc
- Orbits in the galaxy constrained by the “shape” of the potential
- **Measure mass (enclosed) of each galactic component, “map” the potential**
- **Enclosed mass can be traced by velocities!**

Gravitational Potential

- So need to trace...
 - SMBH, bulge, bar
 - Thick disk
 - Thin disk
 - ISM (gas and dust)
 - Halo (stars)
 - Halo (Dark Matter)
- and probably good to consider
 - Arms, density variations
 - Warps
 - Mergers/satellites
- AND worry about inconsistent tracers (i.e. what if gas impacted by heating, other physics, not just $\Phi(r)$?)

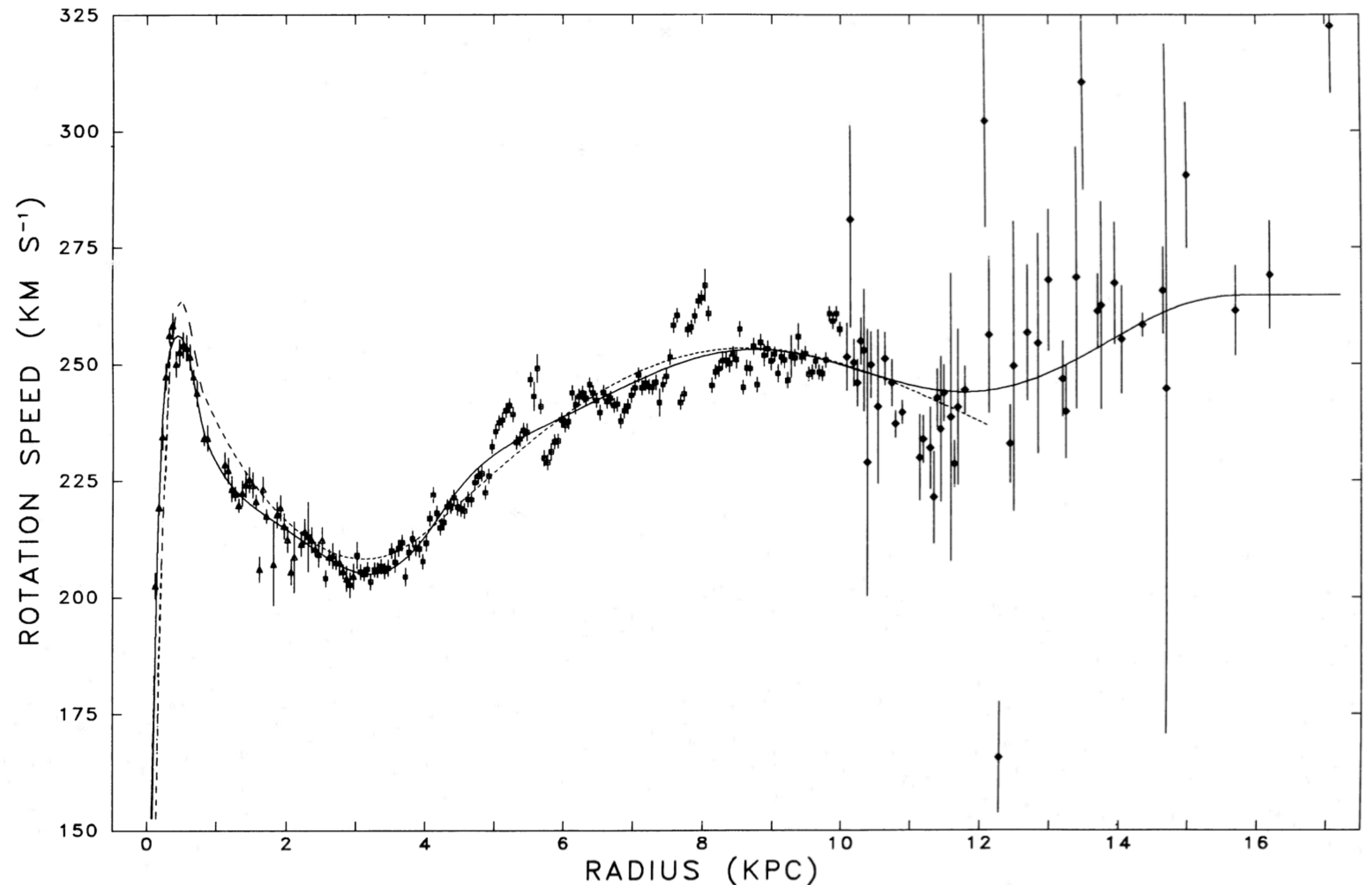
Dark Matter

- Rubin & Ford (1970) a canonical paper on the Andromeda “Nebula” (M31)



Milky Way Rotation Curve

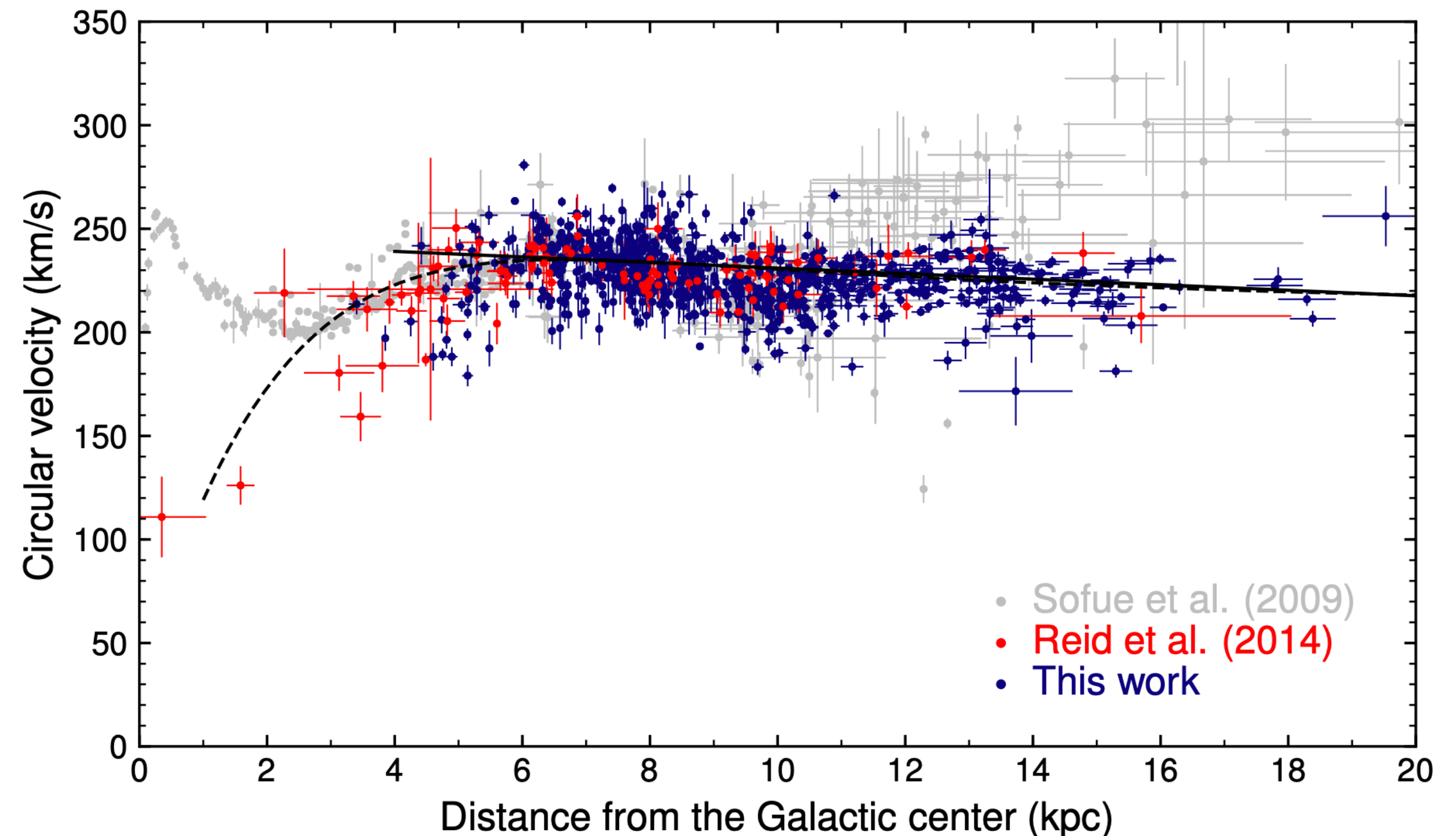
- Gas a useful/classic tracer
 - H I in the nuclear region
 - CO in the middle (near us)
 - H II in the outer regions



Clemens (1985)

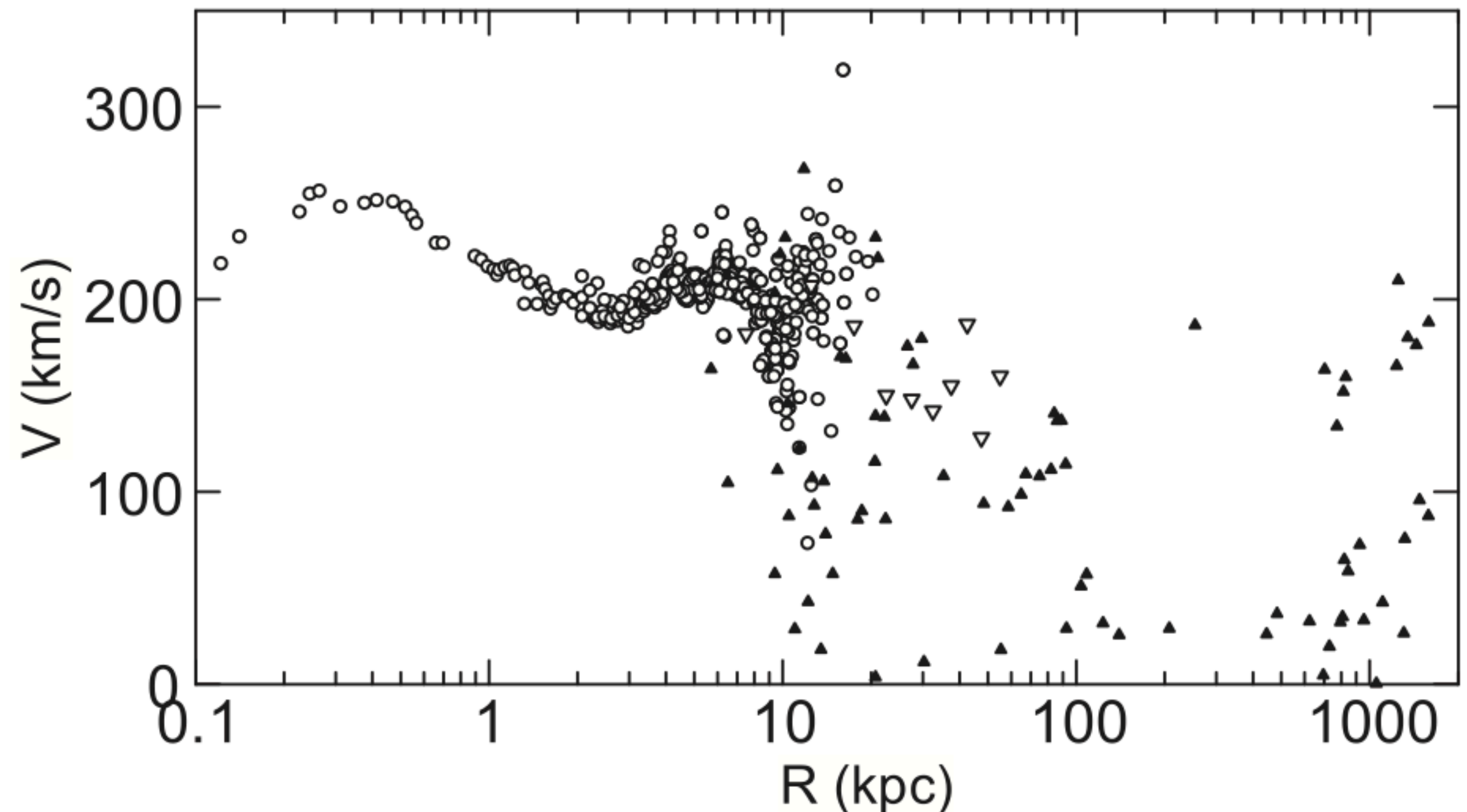
Milky Way Rotation Curve

- Cepheids maybe better for outer disk?
- It's *really* flat... this means DM contribution must contribute a lot in outer disk
- It can't stay flat forever... right?!



The *Grand* Milky Way Rotation Curve

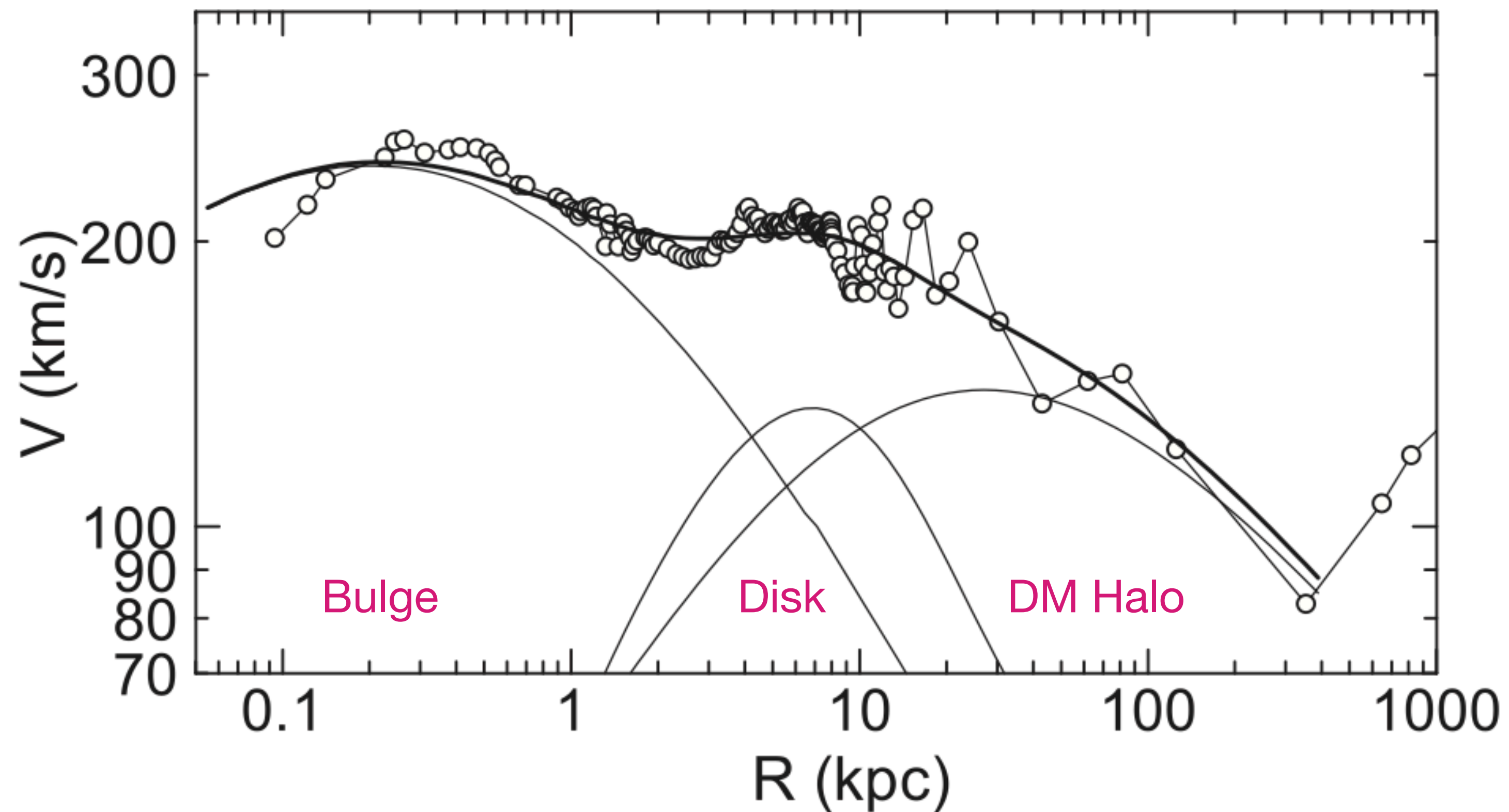
- Combining lots of tracers
- Need long lever arm to really measure the mass distribution contained in the Dark Matter Halo!
- Out to ~ 1 Mpc (!)
 - Note: M31 is < 1 Mpc...



Sofue (2012)

The *Grand* Milky Way Rotation Curve

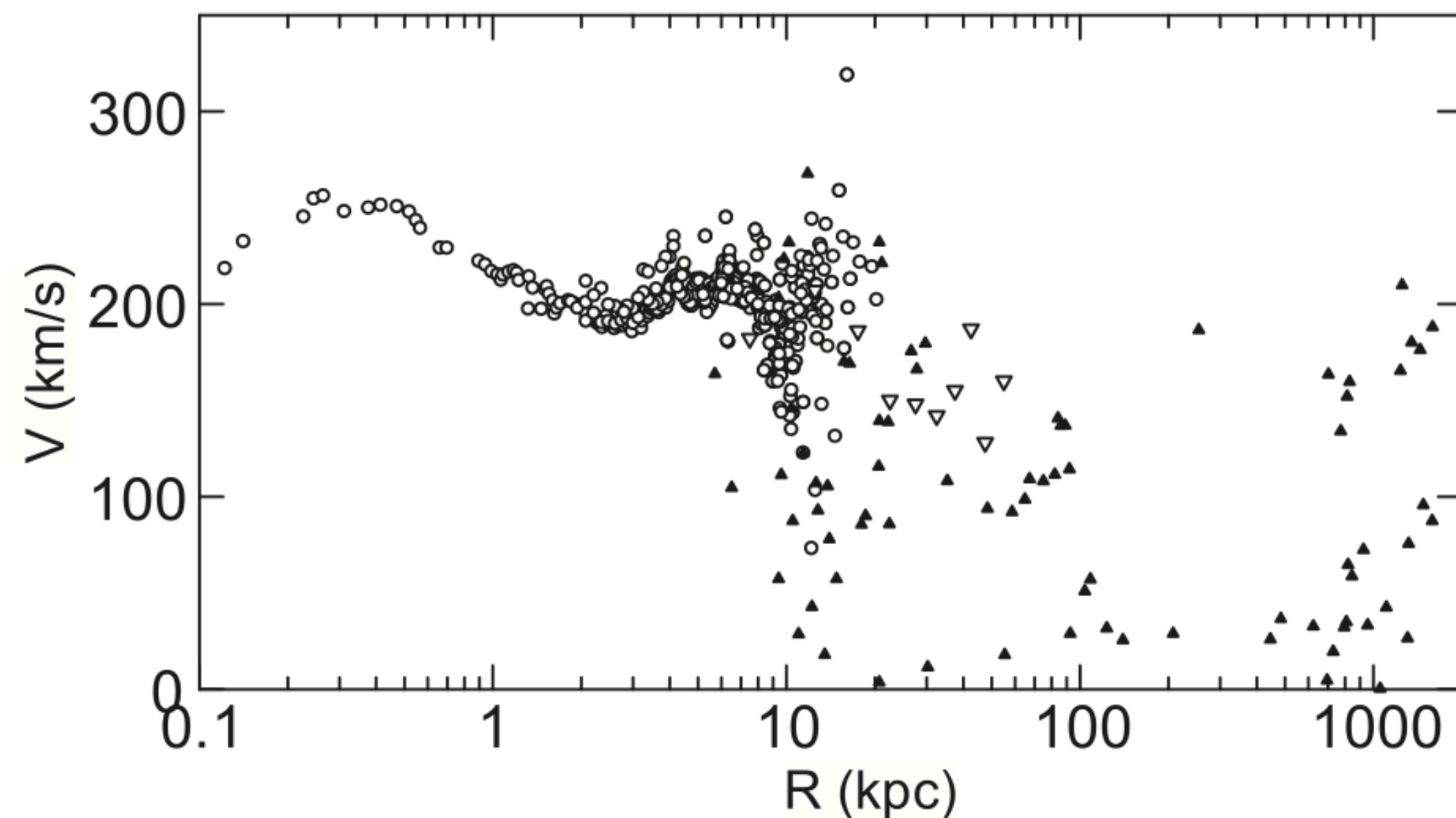
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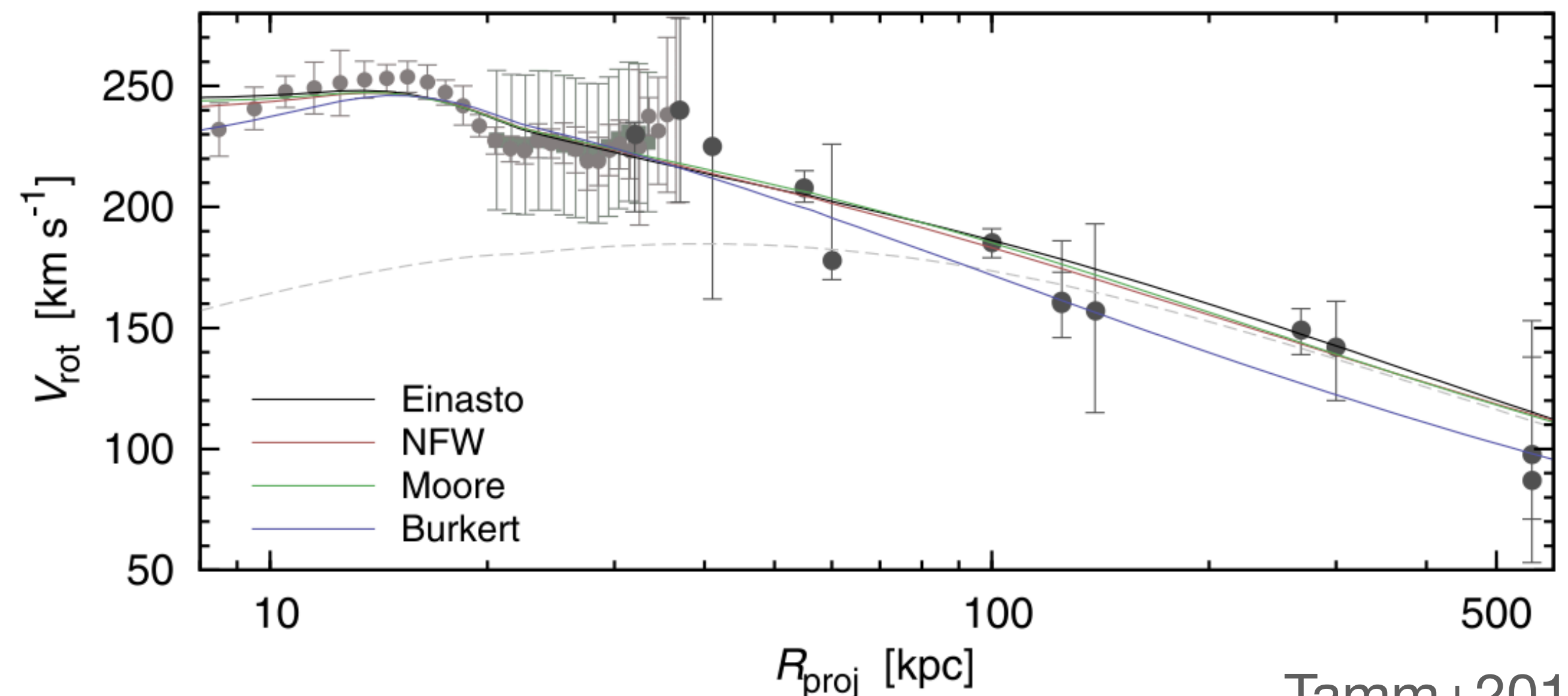
Sofue (2012)

An Aside: The view from 1000 kpc

- Distance is ~ 725 kpc to center of Andromeda
- Milky Way & Andromeda are probably *already* touching!
 - Esp. their DM halos (see rotation curves below)
- Some indication their CGM is already interacting! [Lehner+2020](#)



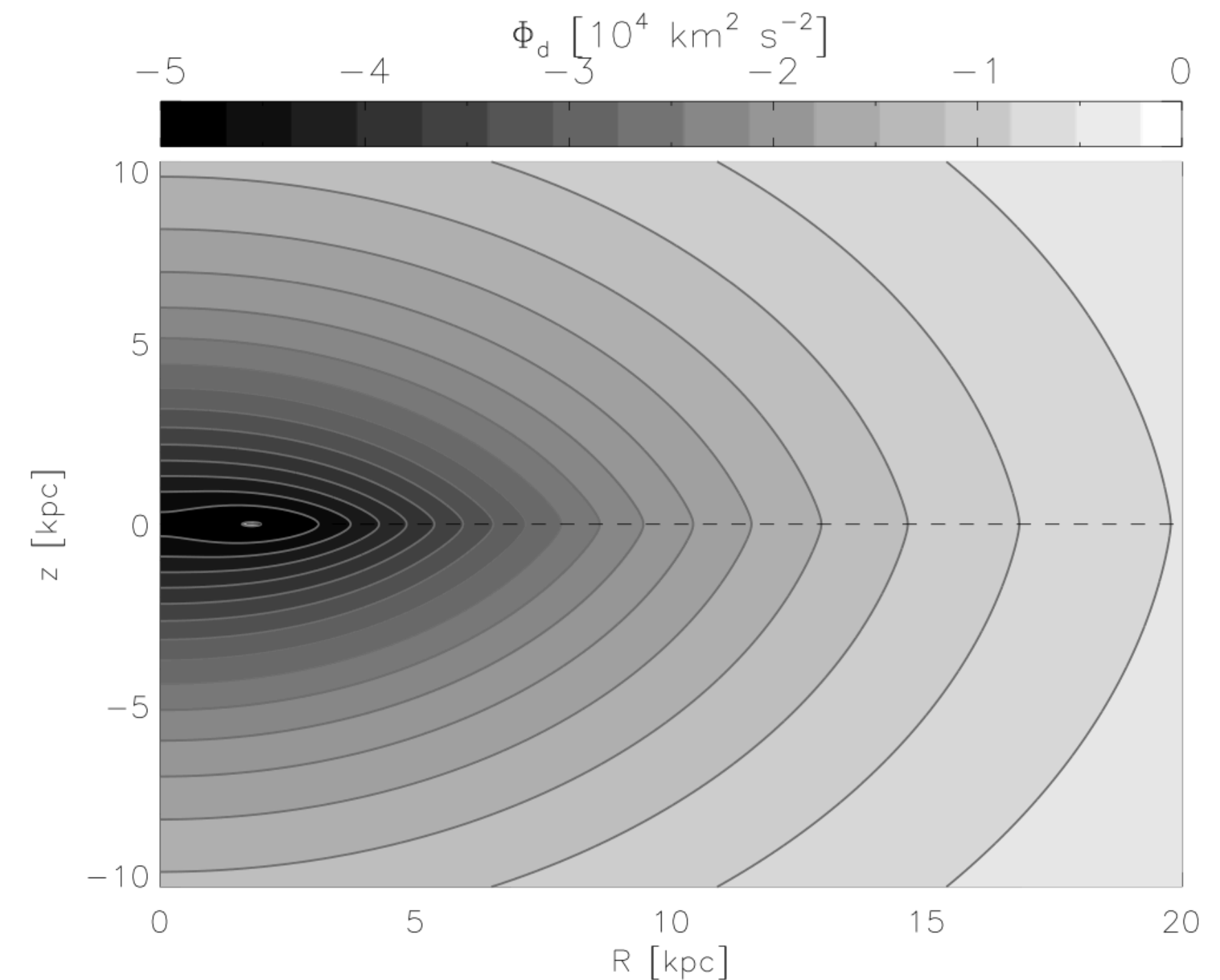
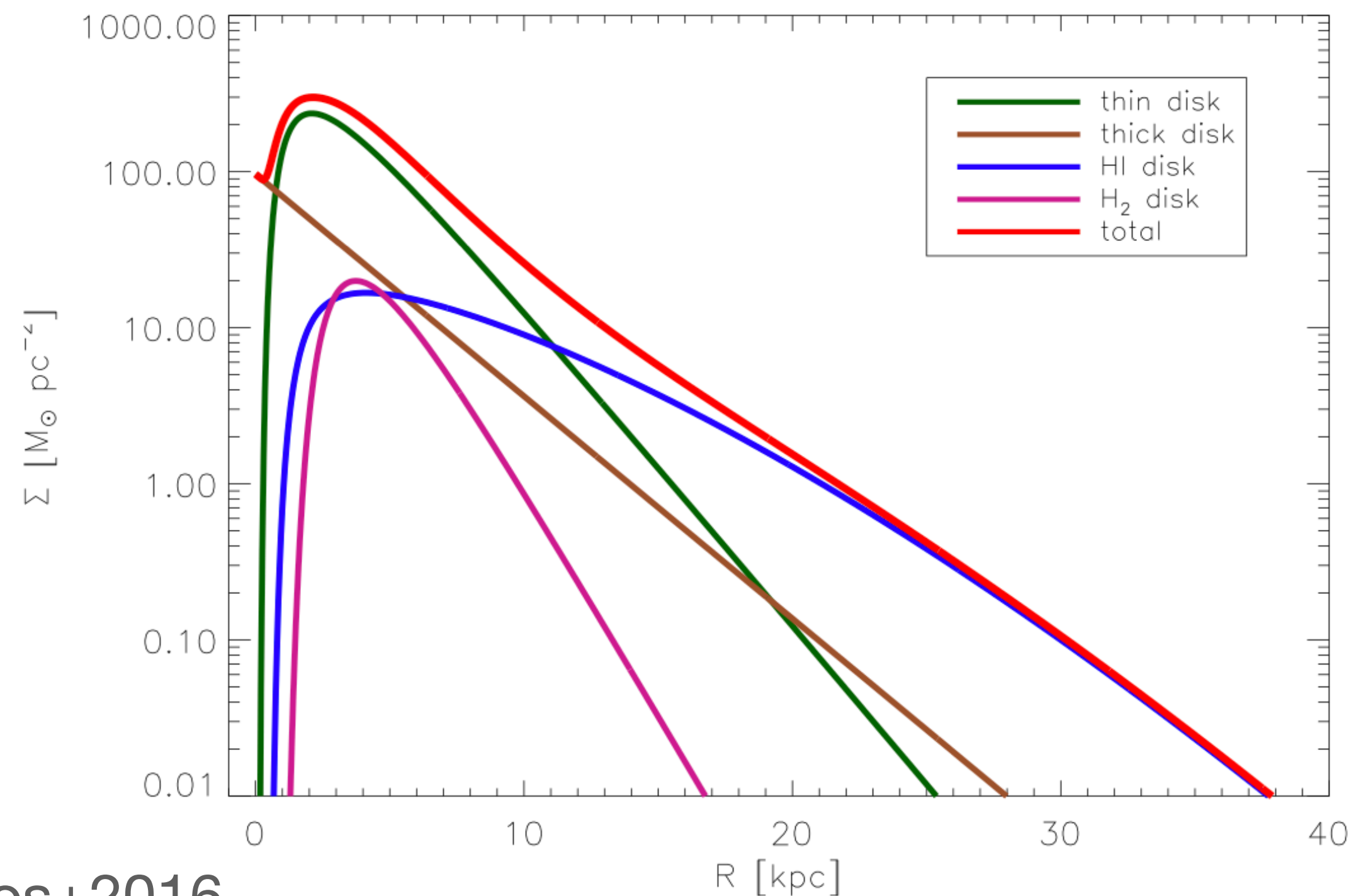
[Sofue \(2012\)](#)



[Tamm+2012](#)

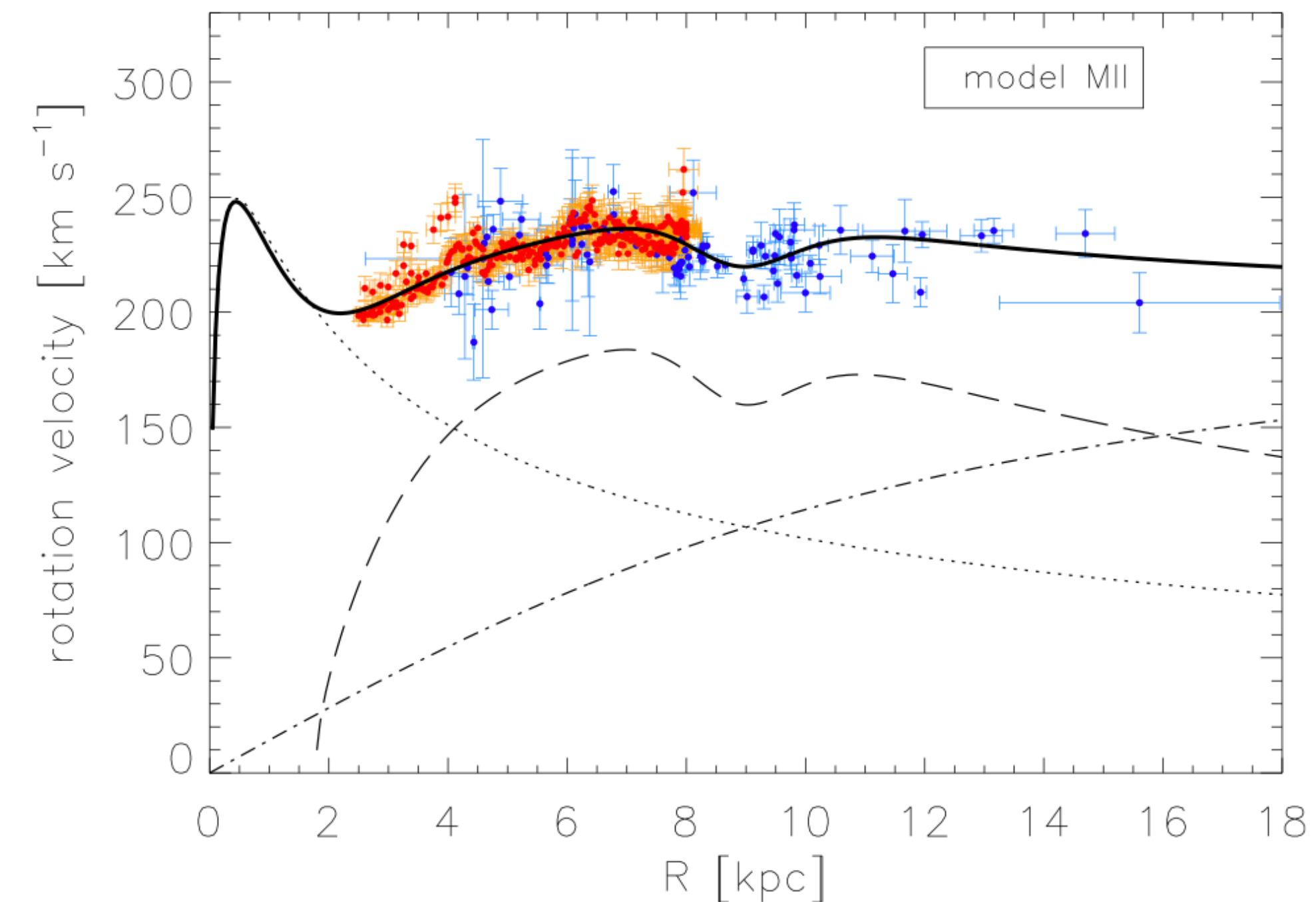
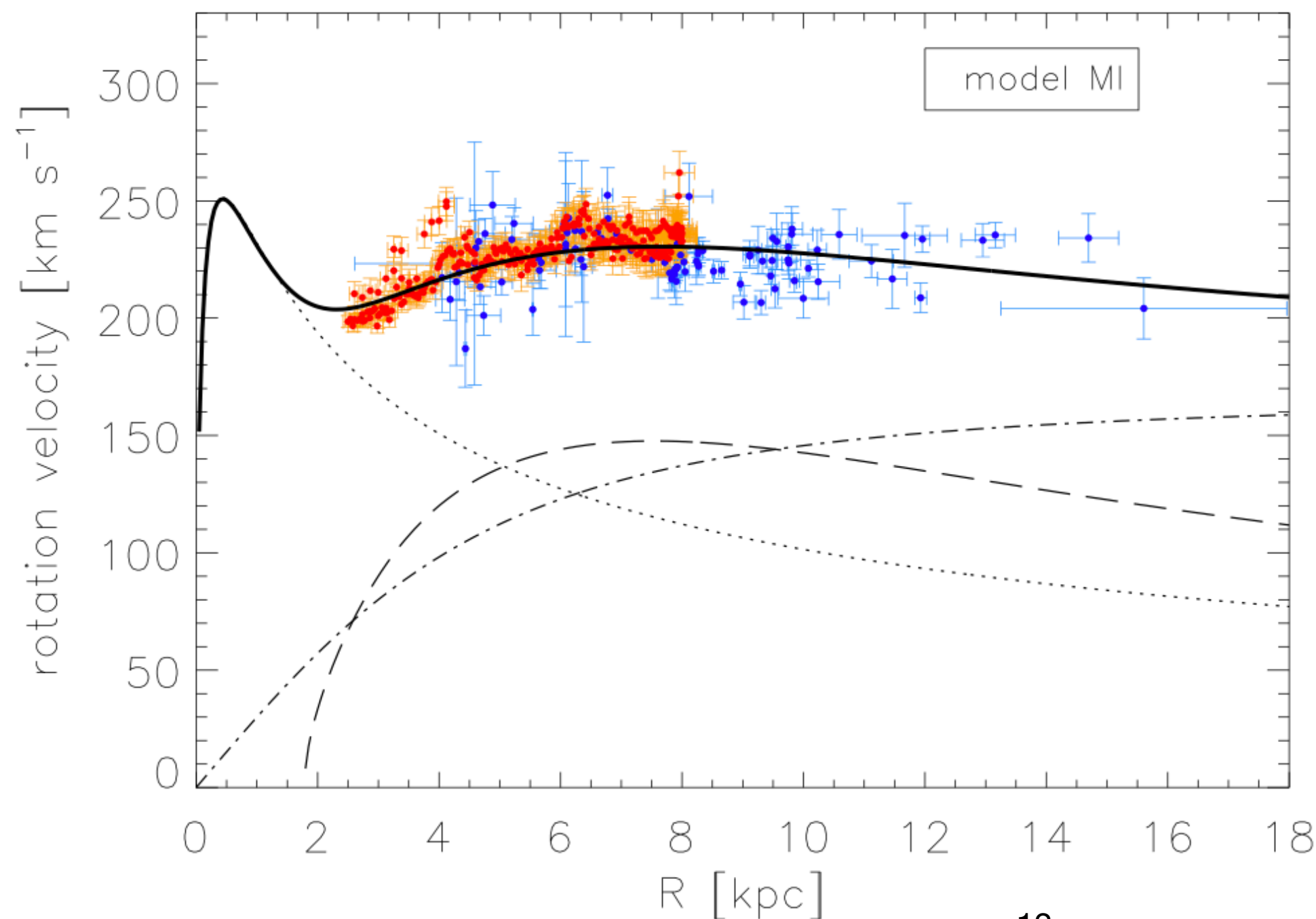
Gravitational Potential of the MWY Disk

- Good, classical models for axisymmetric disk potentials exist (e.g. the Miyamoto-Nagai potential)
- Fit the traced mass distribution of stars and gas pretty well!



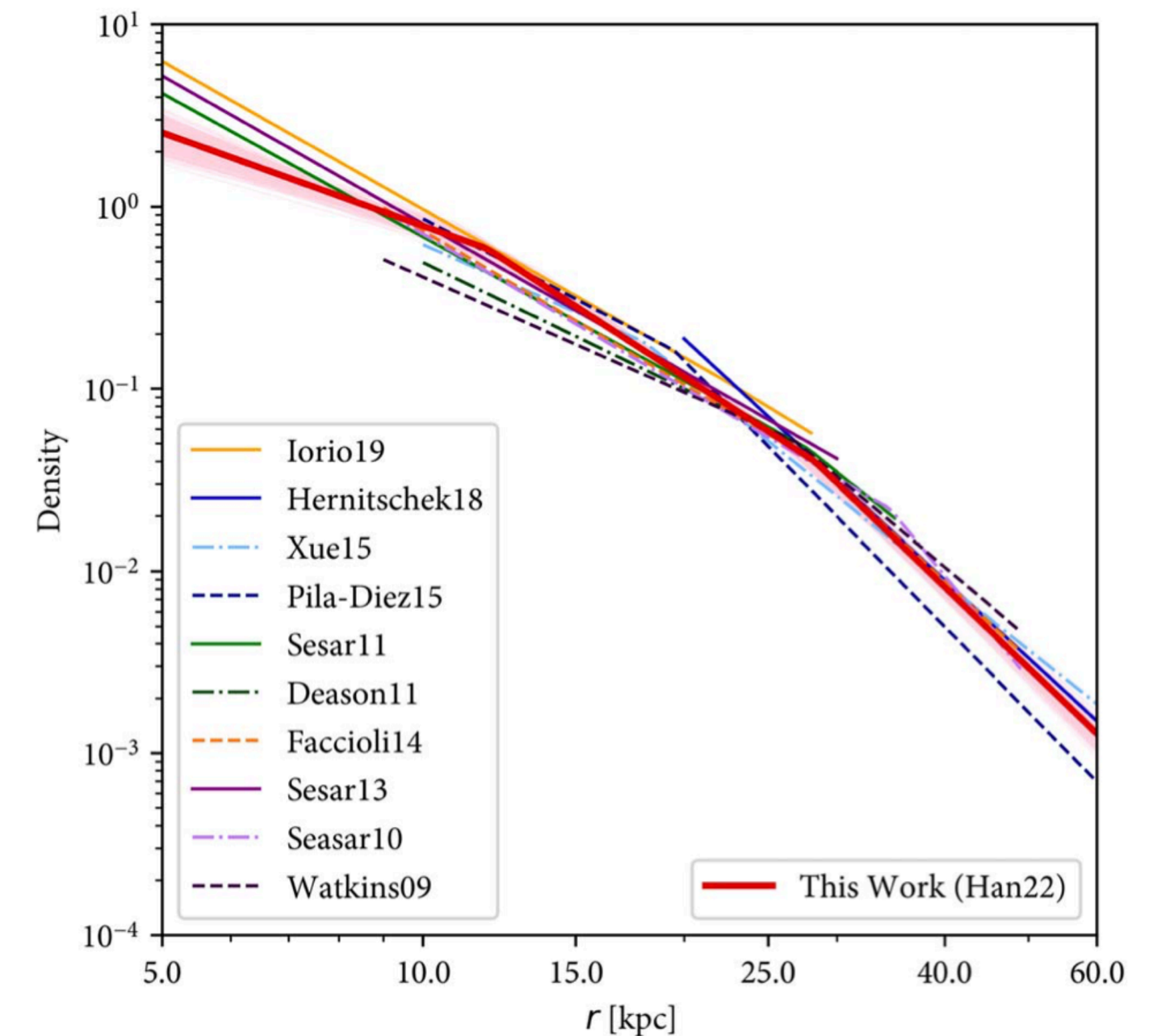
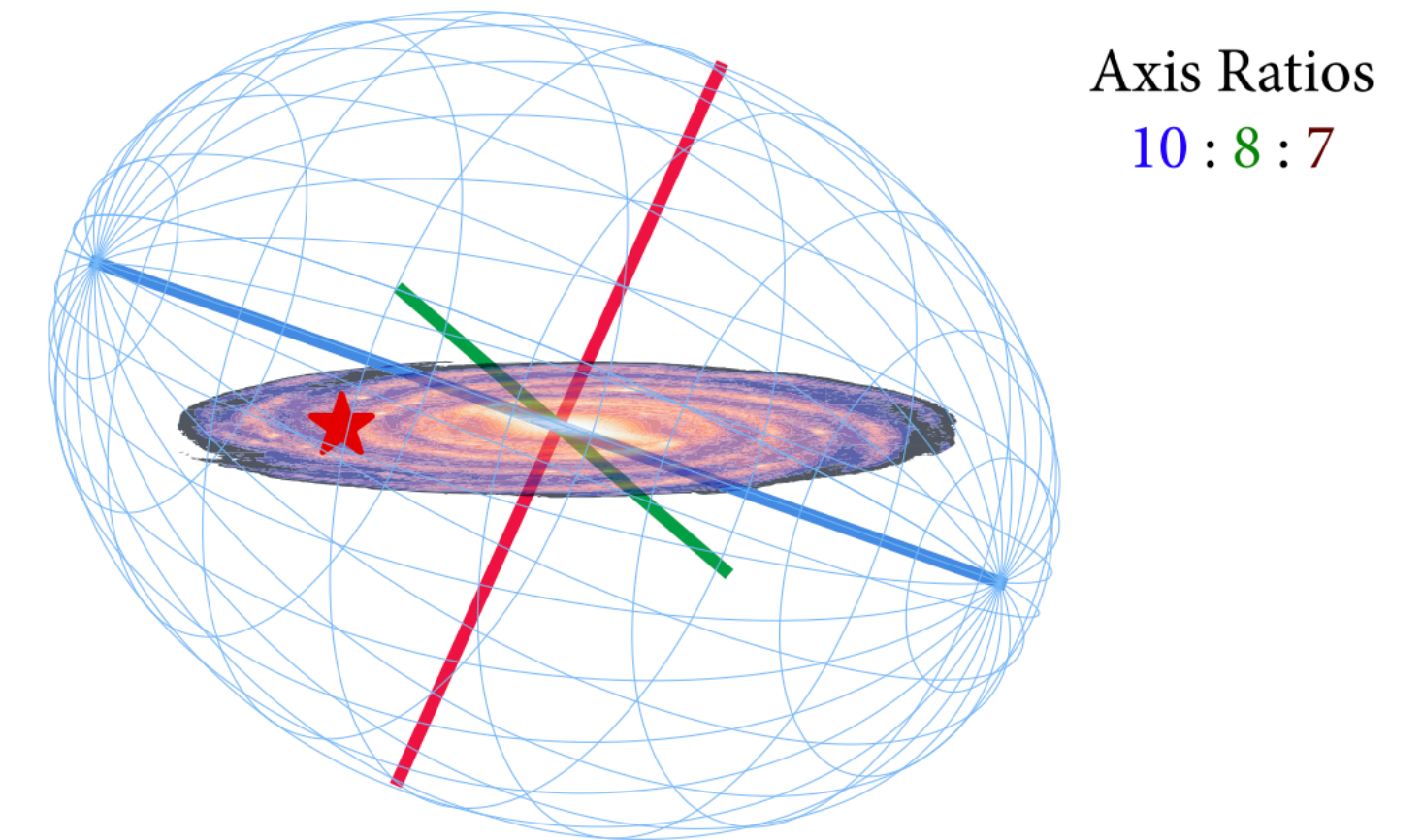
Gravitational Potential of the MWY Disk

- Could the disk have a ring? (M31 has a star forming ring)
- *Could* explain “ripple” in rotation velocity at 8-10kpc
- But also... arms? Local substructure? Need sample outside solar cylinder!
- Haven't yet seen Gaia DR3 evidence for this



Stellar Halo

- Stellar halo is likely tilted and “broken” probably largely due to Gaia-Enceladus Sausage
- Does the DM “feel” that?
- Did the Sausage merger bring Dark Matter (and if so, how has it relaxed into our DM Halo? Theorists, help!)



Han+2022

Dark Matter Halo

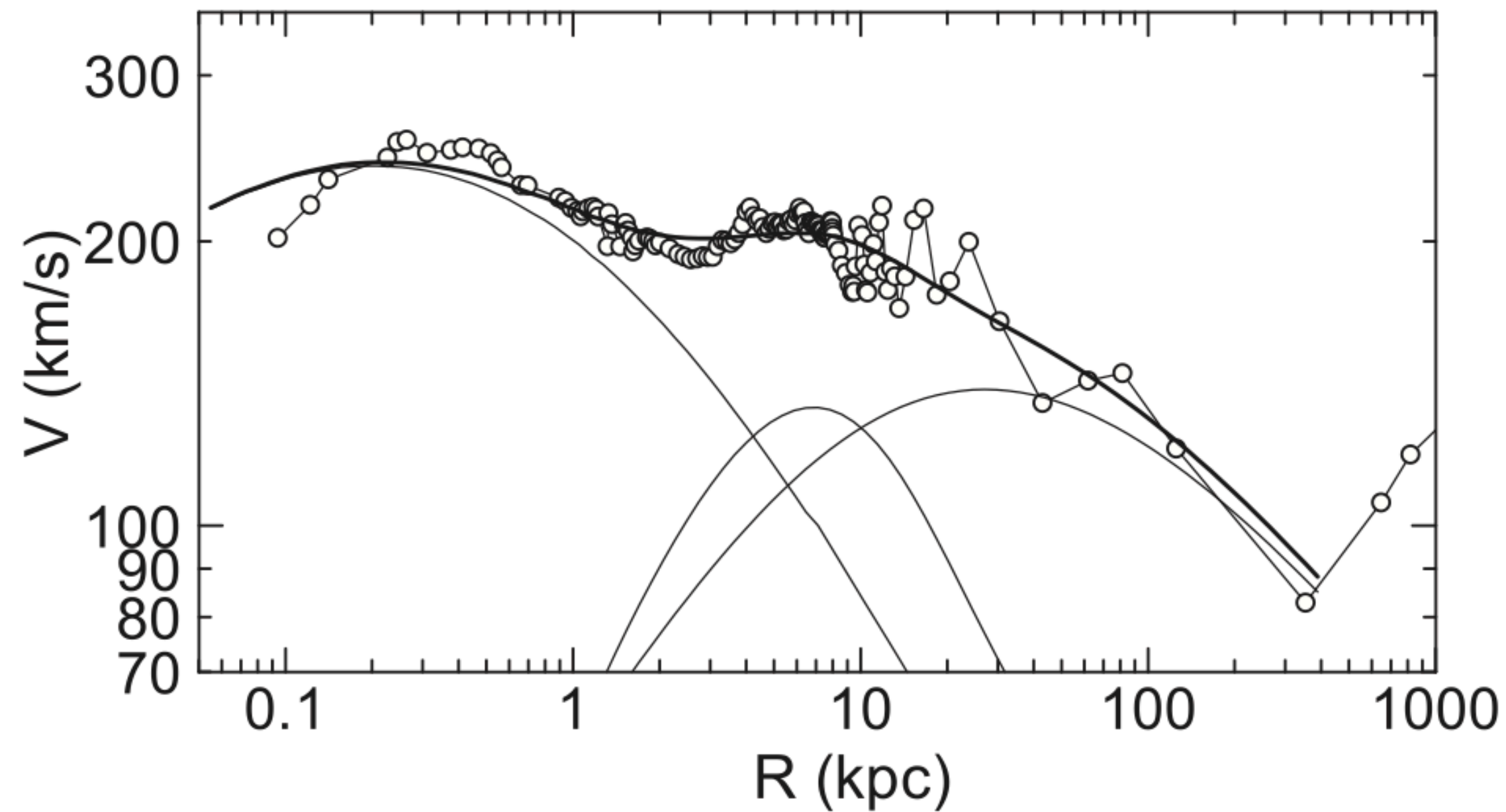
- The now classic cold dark matter potential model:
Navarro, Frenk, and White (1997)
 - *but also laid out in NFW (1996)*
- **Known as an “NFW” profile**
- It’s not the *only* good DM halo profile, but seems to trace mass distributions for galaxies in wide range of sizes, even galaxy clusters!

- $$\rho(r) = \frac{\rho_0}{\frac{r}{R_s} \left(1 + \frac{r}{R_s} \right)^2}$$

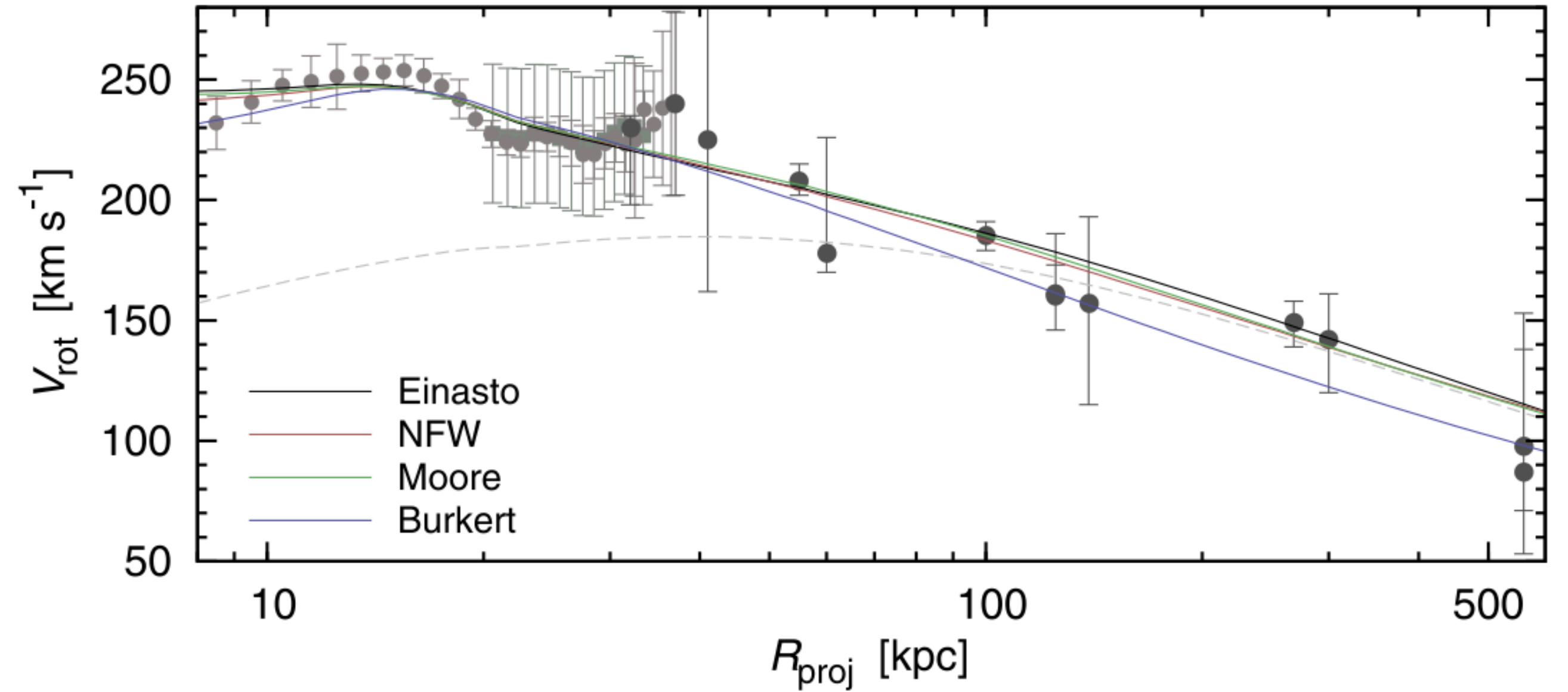
$$\Phi(r) = - \frac{4\pi G \rho_0 R_s^3}{r} \ln \left(1 + \frac{r}{R_s} \right)$$

Dark Matter Halo

- NFW profile works for both MWY and Andromeda out to extreme radii



Sofue (2012)



Tamm+2012

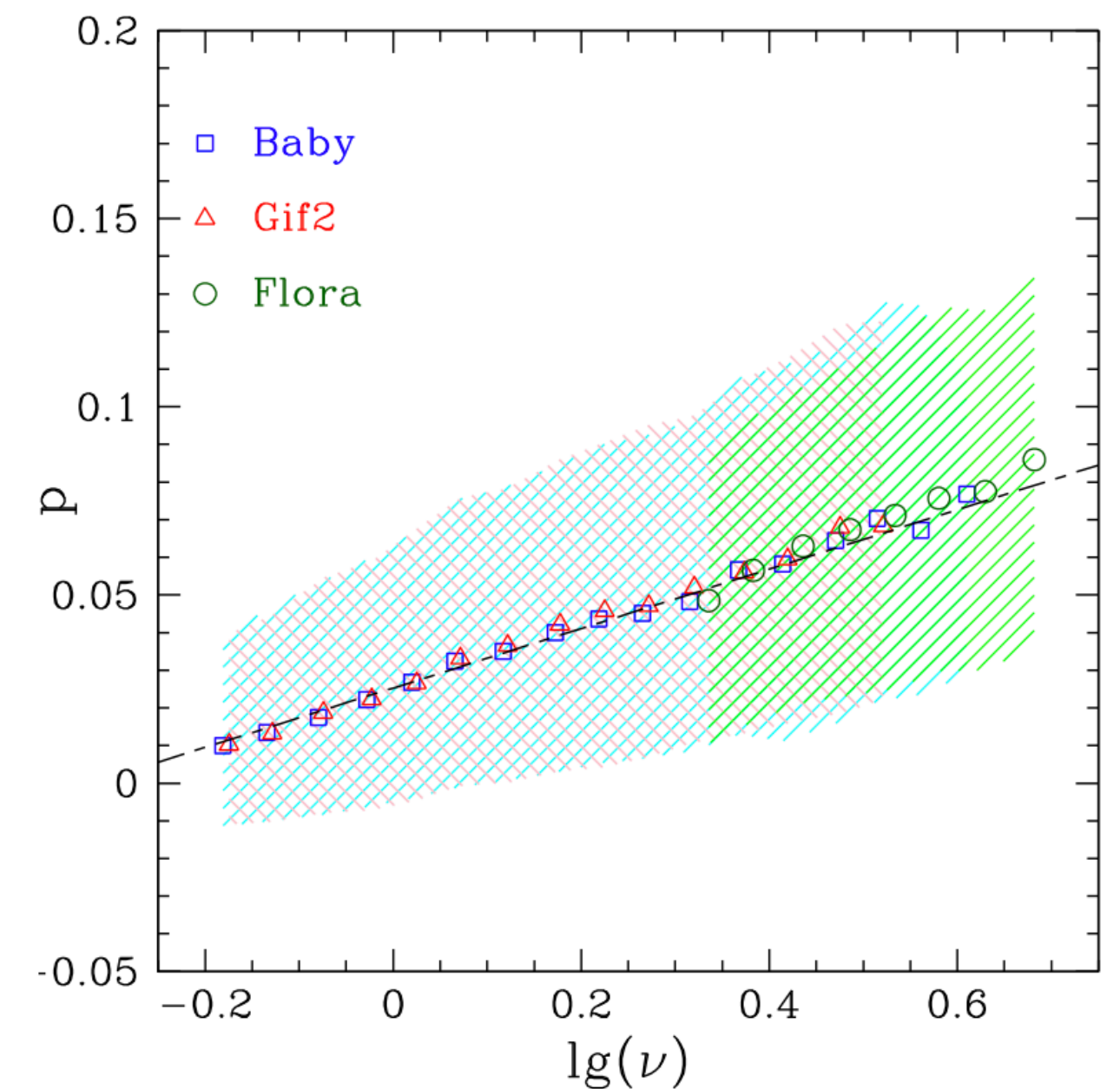
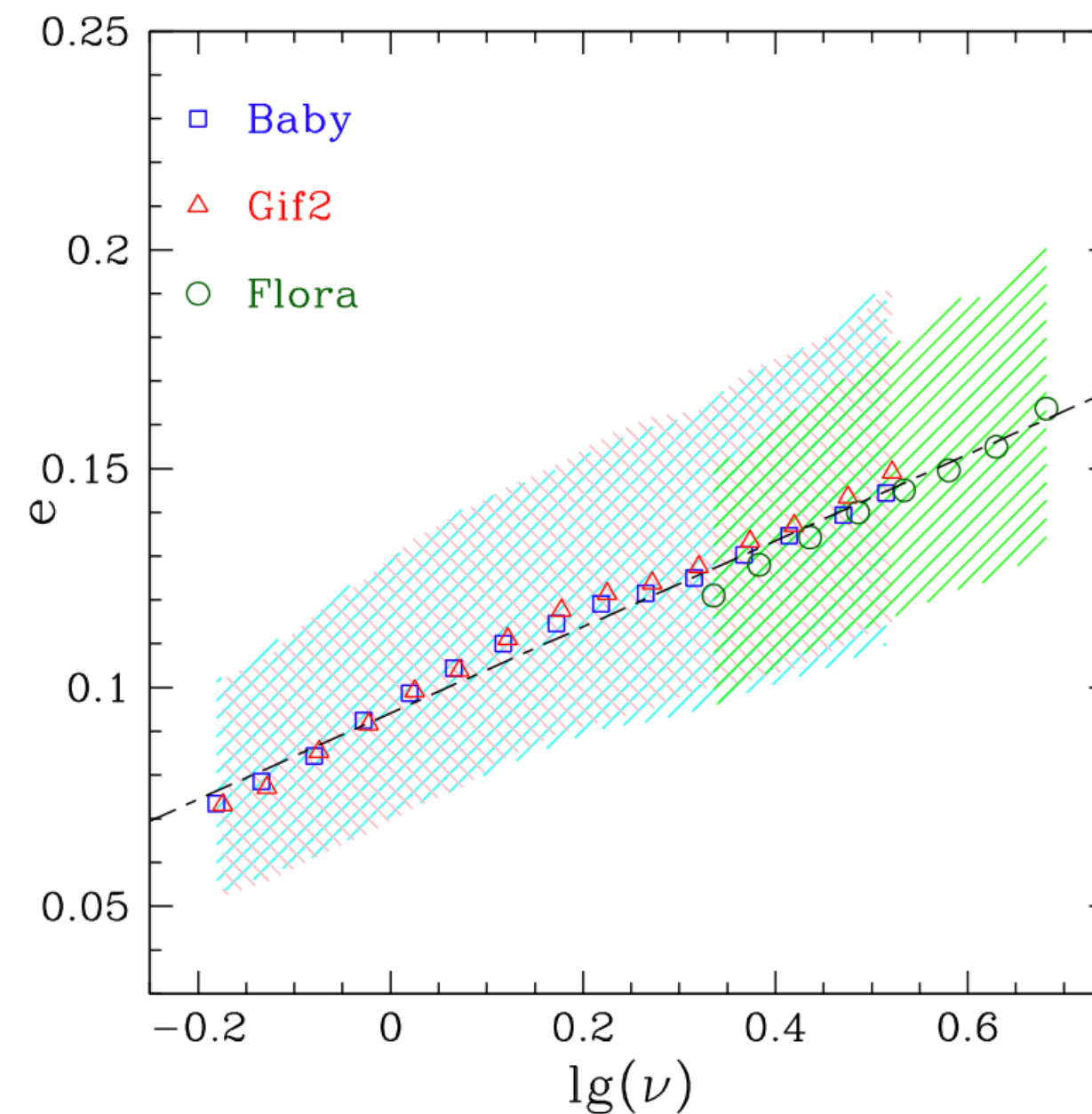
$$\Phi(r) = -\frac{4\pi G\rho_0 R_s^3}{r} \ln\left(1 + \frac{r}{R_s}\right)$$

Dark Matter Halo

- NFW has a few challenges:
 - Predicts high density of DM in the center of galaxies (the “core-cusp” problem), not seen in low surface brightness galaxies
 - Maybe some tension at very large radii for galaxies (small samples)
 - Smooth versus lumpy DM distribution?
 - **Spherical DM halo, versus “triaxial”?**

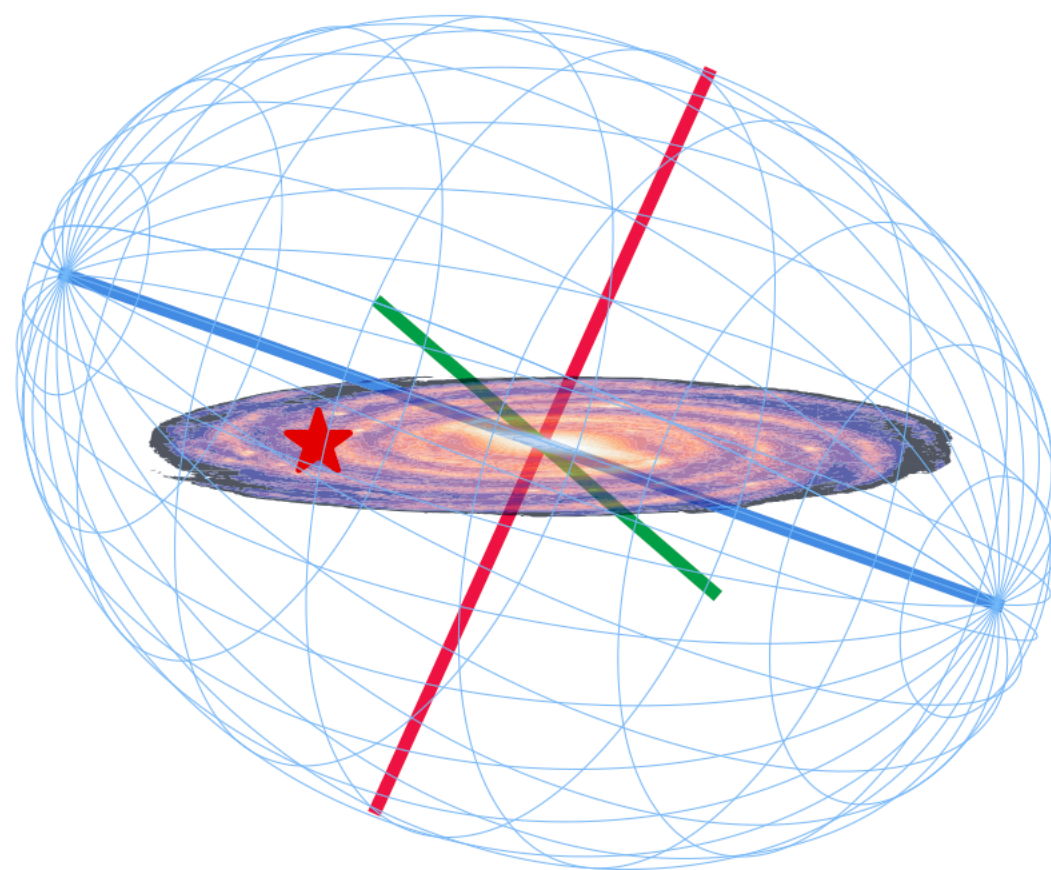
Triaxial DM Halo?

- Simulations can produce triaxial DM halos
- e.g. Giulia+2014, Heller+2007, & many simulation papers...
- DM-only simulations more likely to be triaxial, baryons make halos rounder and more oblate (Chua+2019)



Triaxial DM Halo?

- Some evidence from early models of Sag dwarf spheroidal stream (esp from SDSS) that a spherical DM potential wasn't preferred
- Triaxial DM *seemed* to work better
 - e.g. [Law+2009](#)

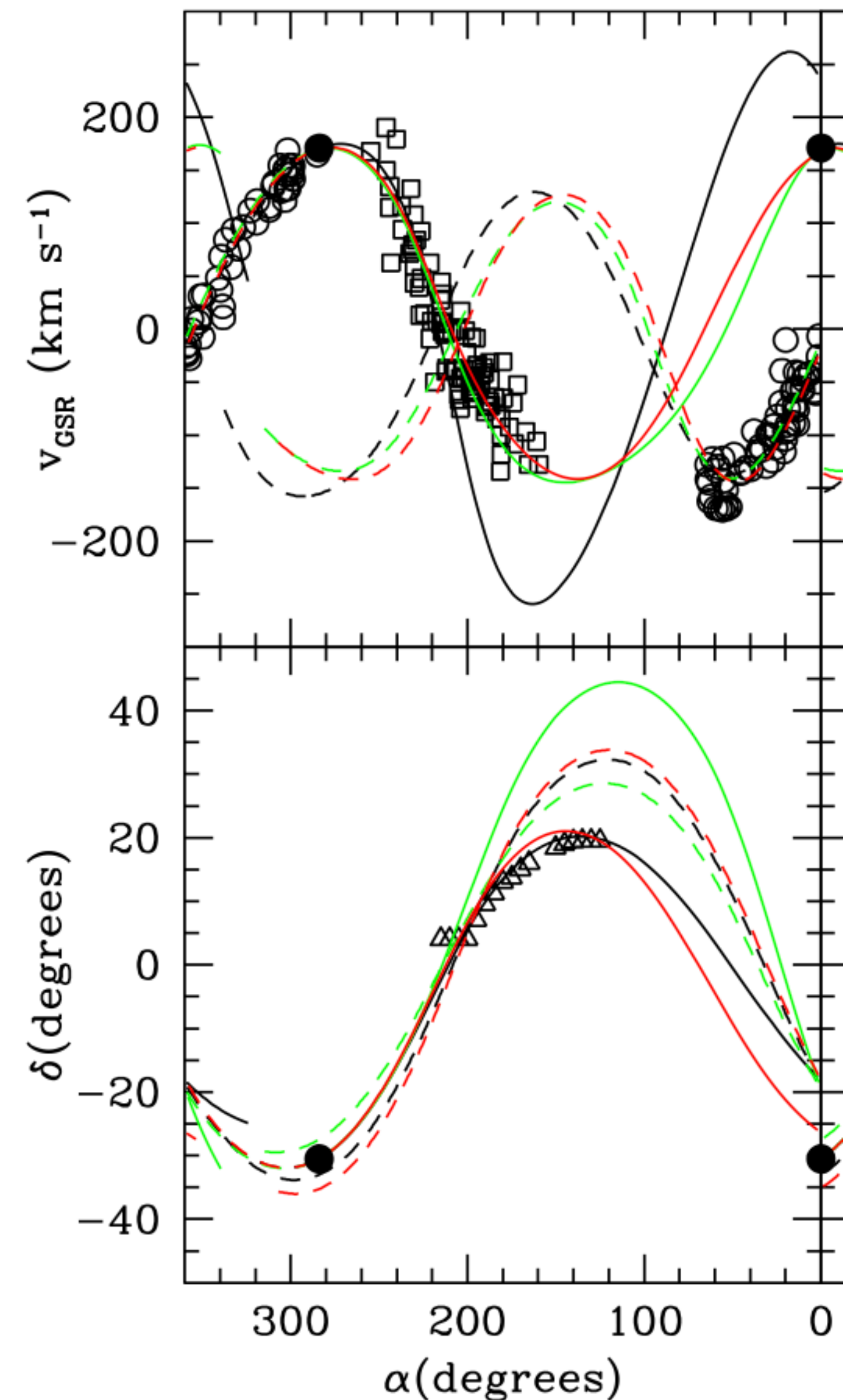


Axis Ratios
10 : 8 : 7

Axisymmetric 1

Axisymmetric 2

Triaxial Halo



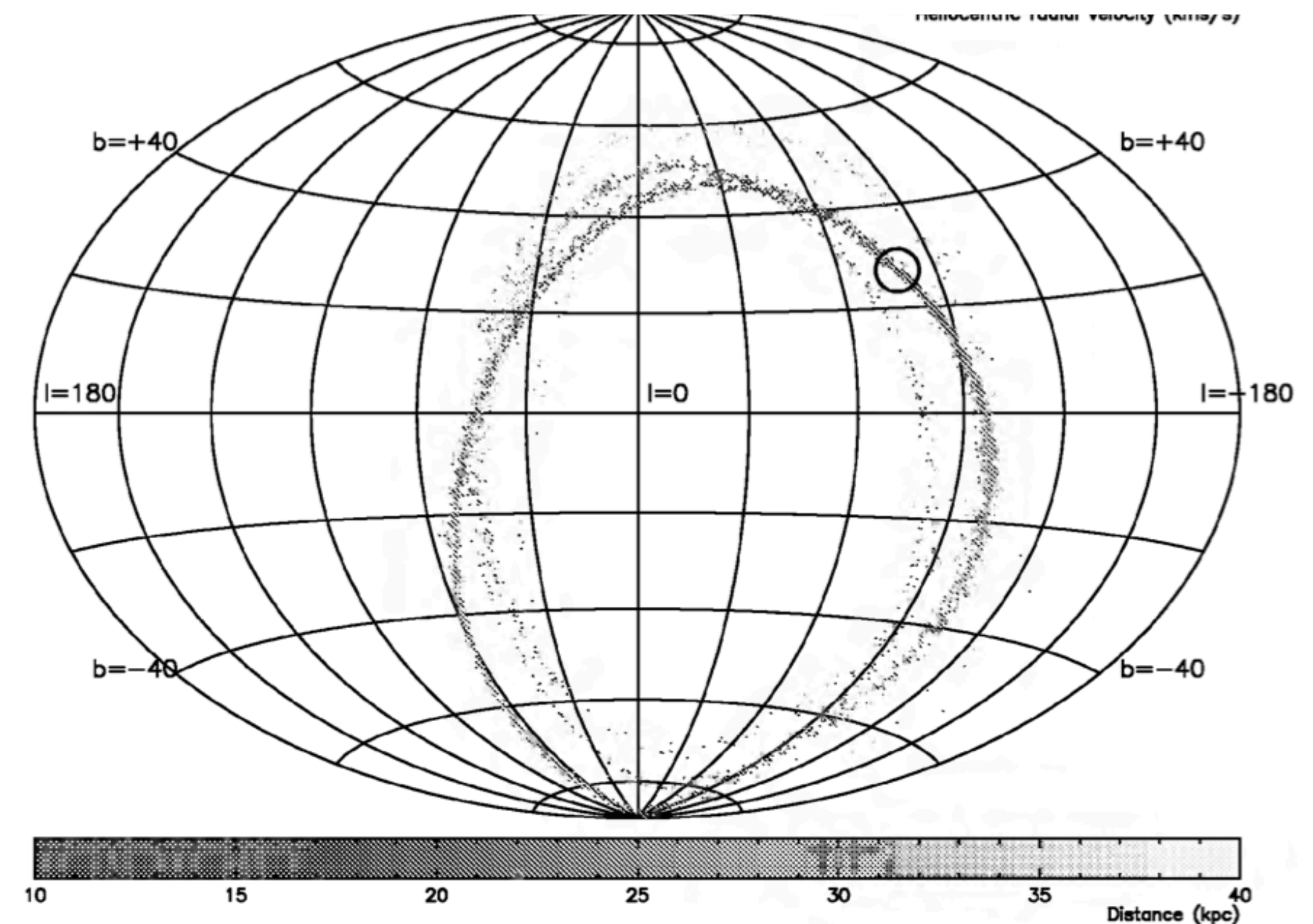
Also recall the stars!... [Han+2022](#)

Tracing the Potential with Streams

- Disrupted clusters or dwarf galaxies can not only trace the entire potential, but help rule out a lumpy DM halo

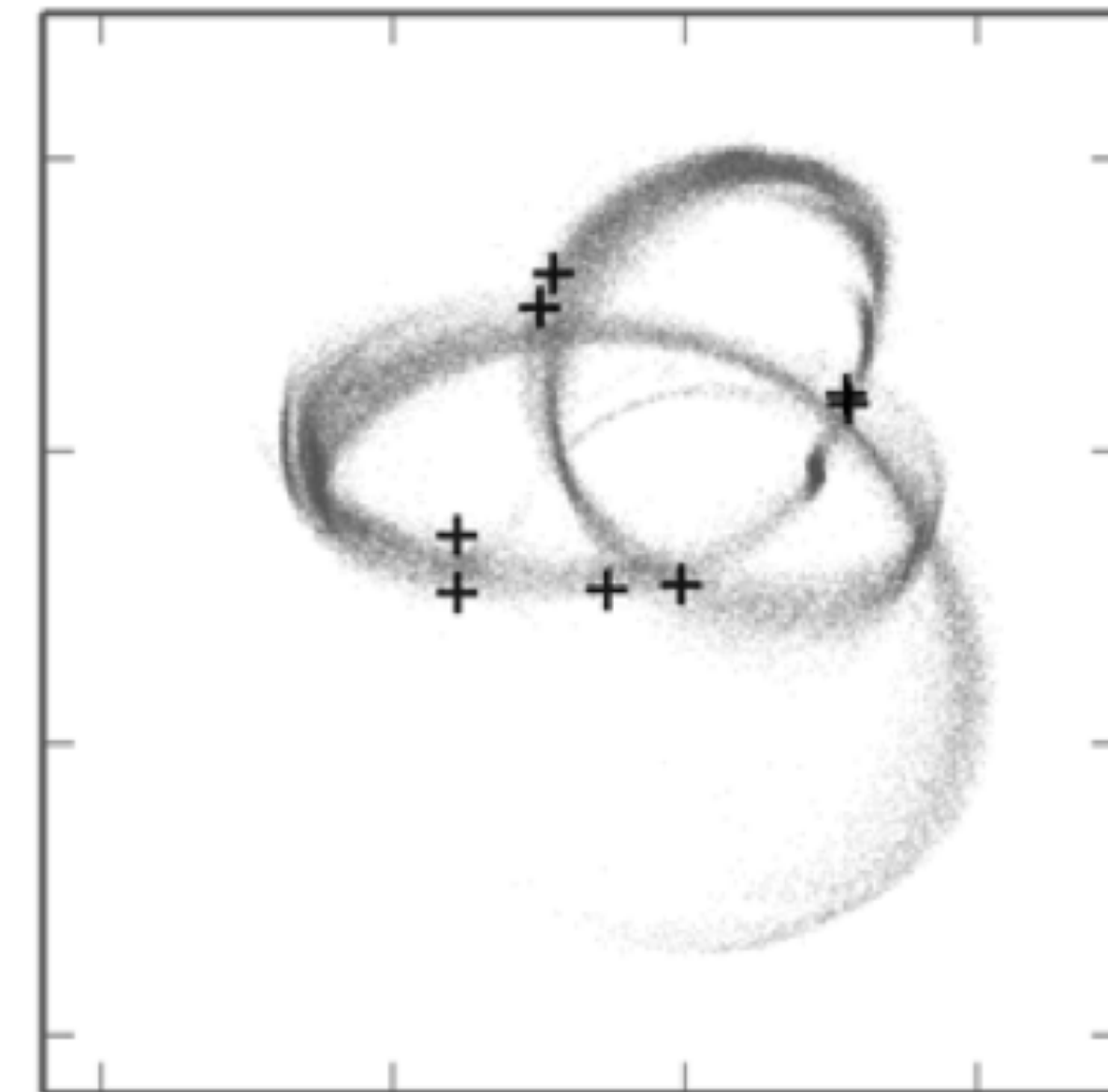
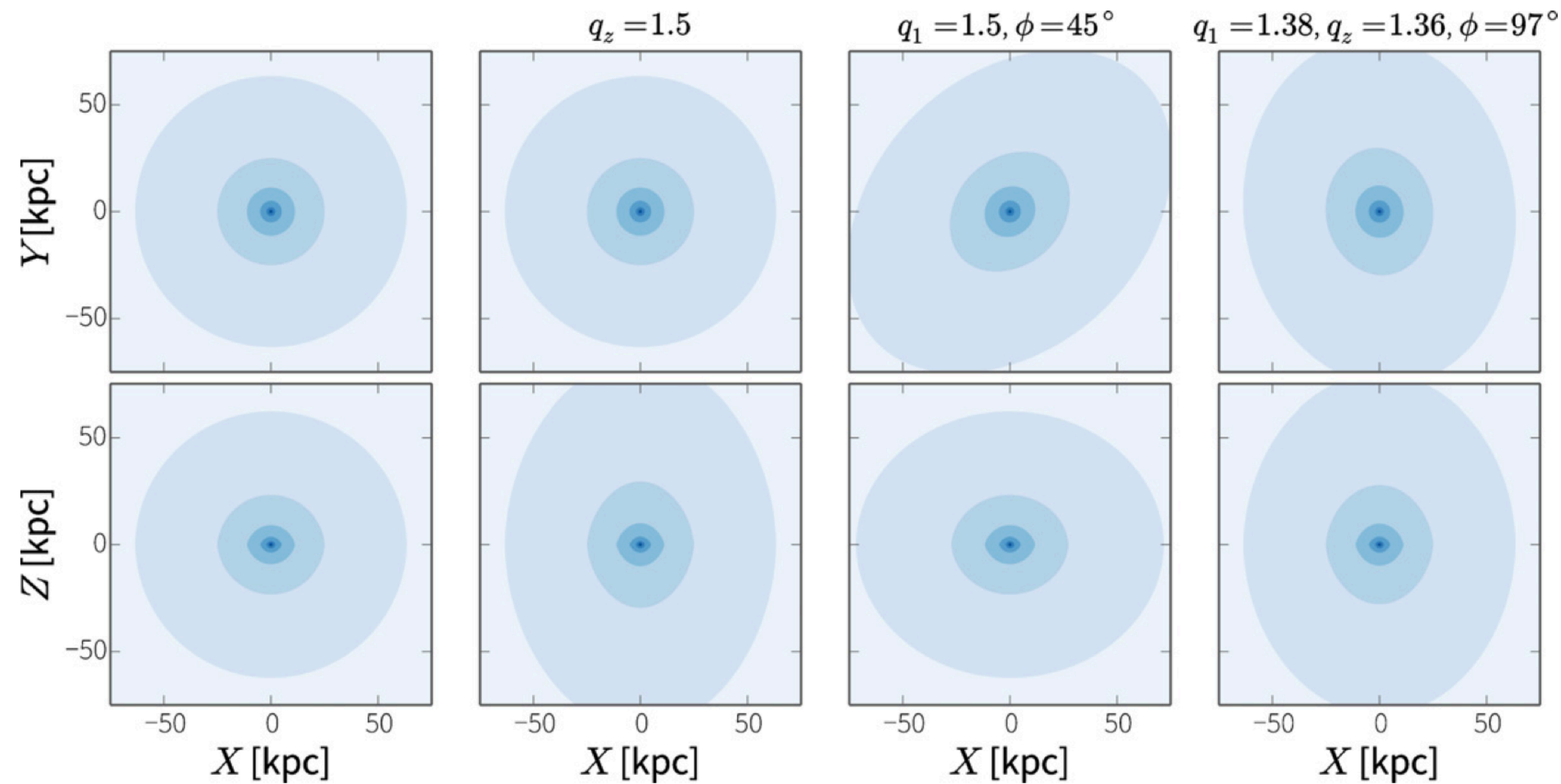
e.g. see [Ibata+2002](#)

This work has shown that from an all-sky survey with high precision astrometry, such as will be obtained with the *GAIA* satellite, we will easily be able to detect globular cluster streams, and measure their kinematic properties, especially the dispersion in L_z .



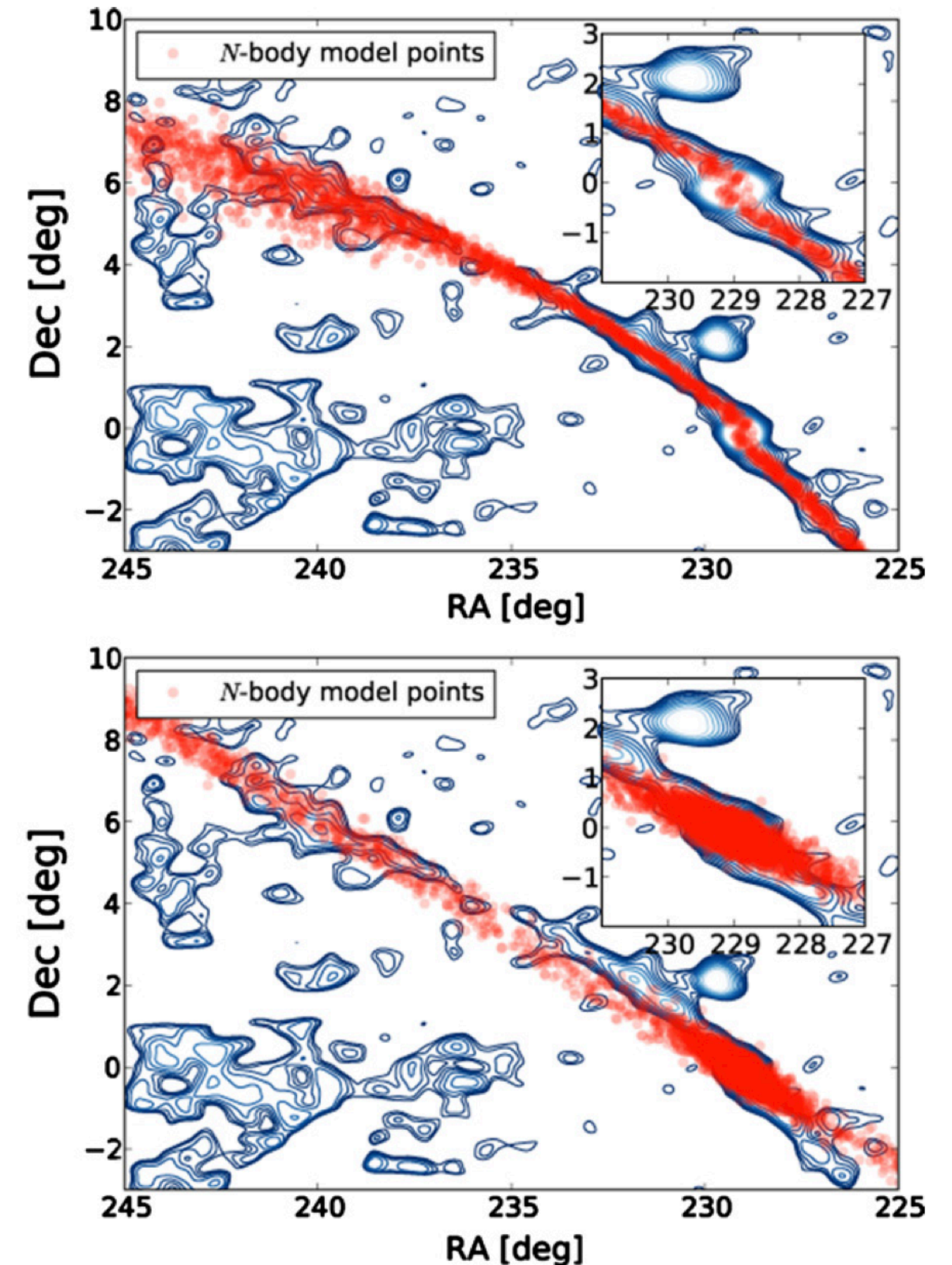
Tracing the Potential with Streams

- Even a small # of stars w/ precise orbital elements can constrain the DM potential profile! Price-Whelan+2014



Tracing the Potential with Streams: Pal 5

- We've looked at this famous tidal stream before (see Lecture 4)
- Very useful for constraining Φ because so well sampled, system is “small” compared to galaxy mergers
- Spherical DM halo (+ realistic disk) model does a good job of reproducing both broad stream profile *and* nuclear “S” shape
- Triaxial shows *lots* of problems for stream
- Pearson+2015

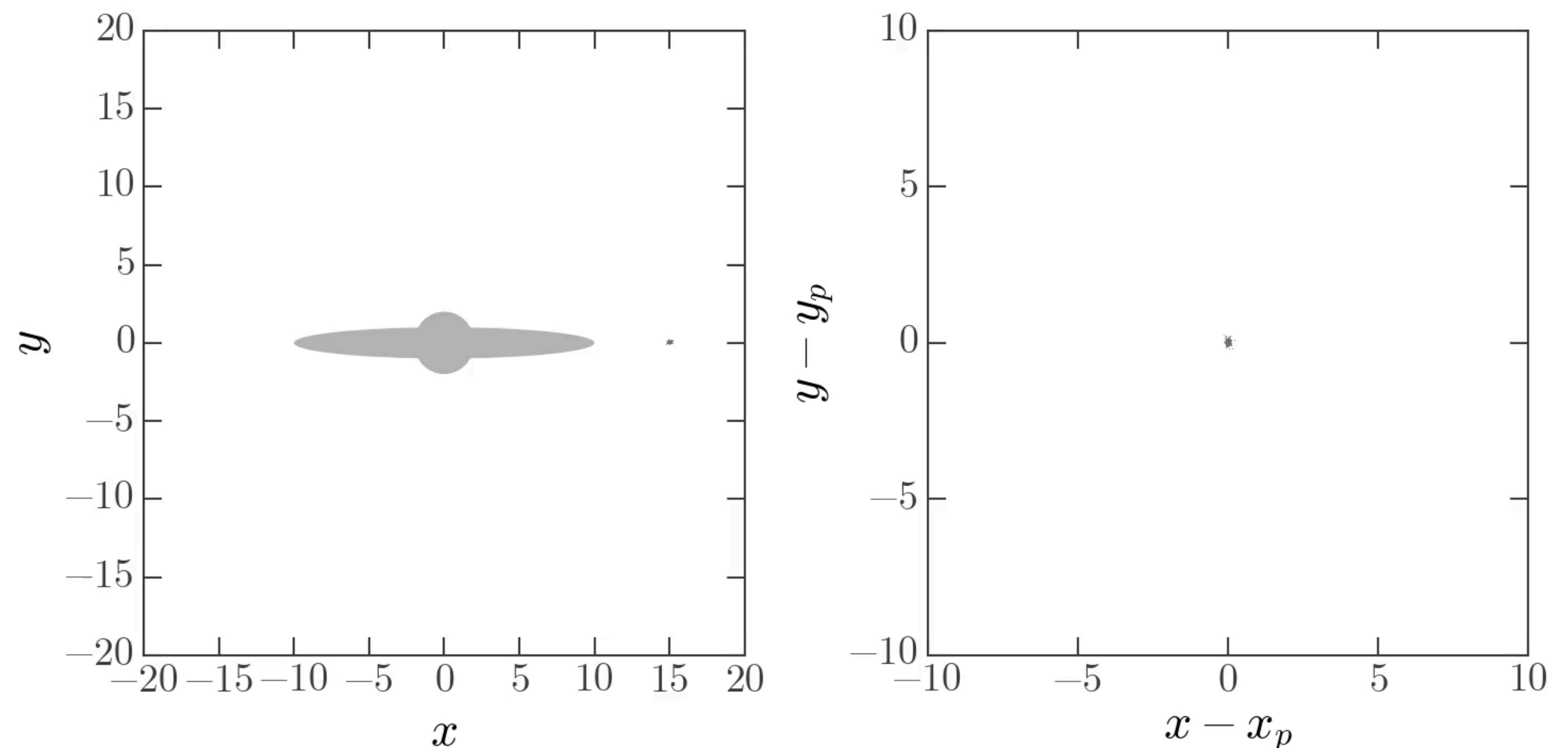


Spherical halo

Triaxial halo

Homework 4: *Destroy This Cluster*

- You lovingly characterized a cluster in Homework 2, explored a bit of the Galaxy it lives within in Homework 3...
- Now I want you to “destroy” it, i.e. try and turn it into a tidal stream!
- This is the final HW!
- Gala package suggested
Could also do with e.g. Galpy



Homework 4: *Destroy This Cluster*

- Try MWY versus NFW potentials... can you destroy your cluster?!
- Two approaches you might explore here:
 - Do lots of orbits w/ small range of initial locations
 - Use a stream-generating prescription

