

ASTR 421

Stellar Observations and Theory

Lecture 09

Line Profiles: II

Prof. James Davenport (UW)

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Today

- Details of line broadening mechanisms
- Ca II HK
- Revisiting other line profiles (P Cygni)



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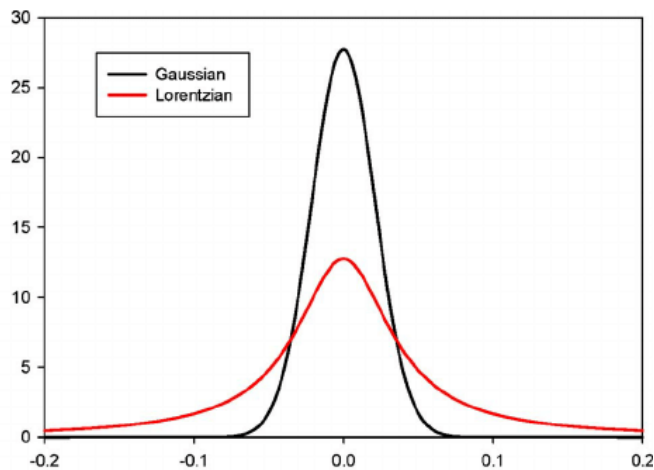
Overview of Line Broadening

Many things can impact “doppler broadening”, anything w/ gas velocities

- Doppler broadening (thermal motions)
- Natural broadening (Heisenberg uncertainty)
- Pressure broadening (a few kinds)

Gaussian profile

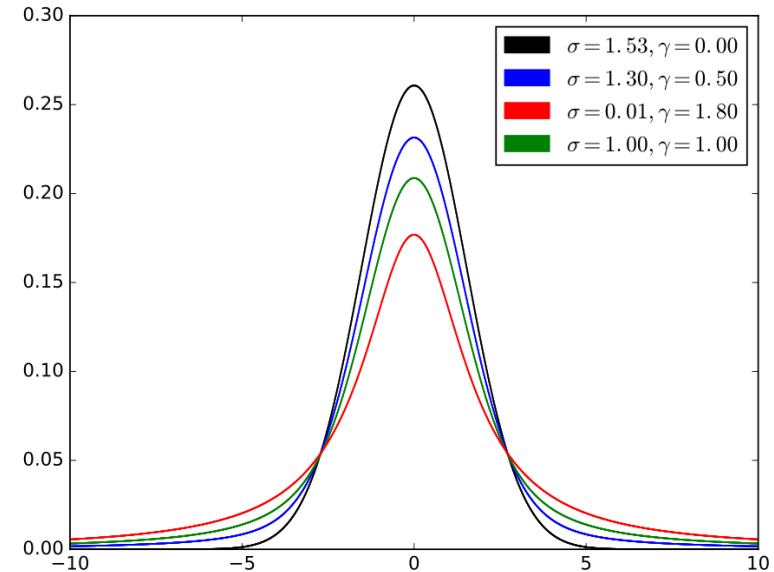
Lorentzian profile



The Voigt Profile

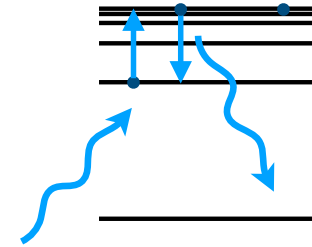
- A *convolution* of Gaussian & Lorentzian profiles
- This the classic line profile equation we use in most cases
 - Core: mostly Gaussian shape
 - Wings: mostly Lorentz shape
- **Useful for constraining physics behind both thermal & pressure broadening in a line!**

$$V(x; \sigma, \gamma) = \int_{-\infty}^{\infty} G(x'; \sigma) L(x - x'; \gamma) dx'$$



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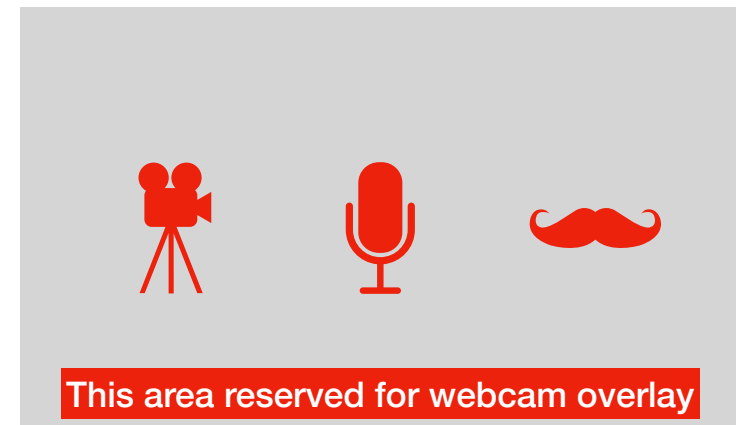
Natural broadening



- Arises due to Heisenberg uncertainty principle
 $\Delta E \Delta t \approx \hbar$
- Time electron spends in excited state is finite... the photon *does* get emitted!
- Plugging in the classic $E = hc/\lambda$ for photon...
- BOB gives estimate of the line width for natural broadening of:

$$FWHM = \frac{\lambda^2}{\pi c \Delta t} \quad (\text{eqn 9.61})$$

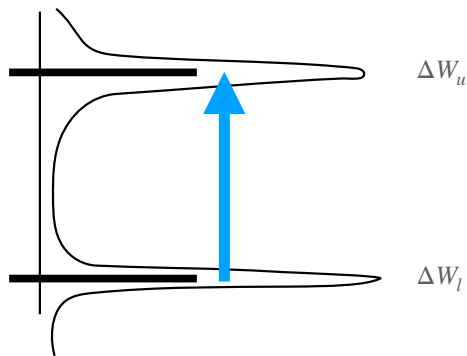
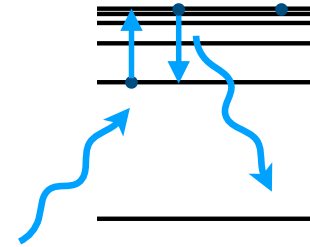
- Example for $H\alpha$: $FWHM \sim 2 \times 10^{-5} \text{ nm (!)}$
- **TYPICALLY VERY SMALL**



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Natural broadening

- Arises due to Heisenberg uncertainty principle
 $\Delta E \Delta t \approx \hbar$
- Another way to think about this is the *location* of the energy levels cannot be precisely determined at any given moment.



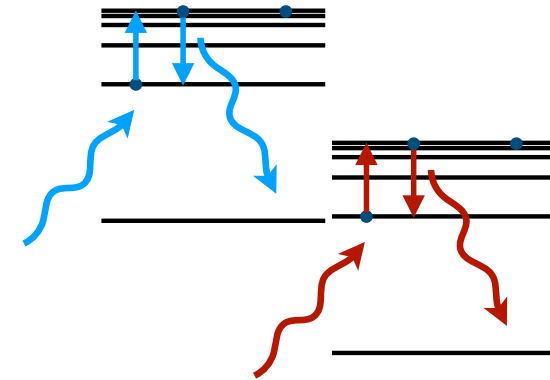
Gray, Fig 11.1



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Thermal (Doppler) broadening

- Arises due to atoms *moving around* in the medium
- Each transition (absorption or emission) is blue/red shifted due to simple doppler velocity shift
- **The line width is therefore determined by the velocity distribution**



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Thermal (Doppler) broadening

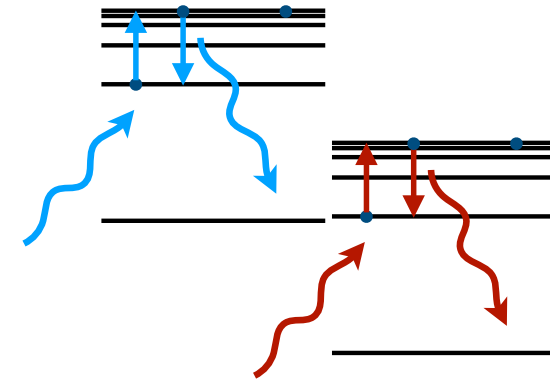
- Thankfully we have a good model for velocity distribution of an ideal gas... our friend once again, the Maxwell-Boltzmann distribution, which classically gives

$$v_{peak} = \sqrt{2kT/m}$$

- A handy reminder for Doppler shift: $\frac{\Delta\lambda}{\lambda} = \frac{v}{c}$
(in non-relativistic limit)

- This yields good approximation of:

$$\Delta\lambda \approx \frac{2\lambda}{c} \sqrt{\frac{2kT}{m}}$$

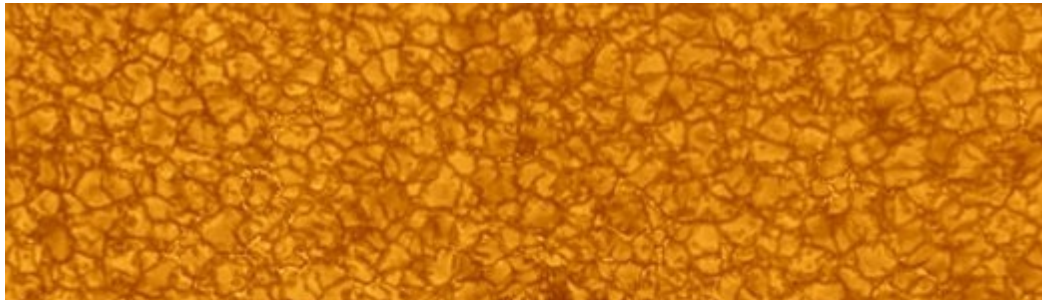
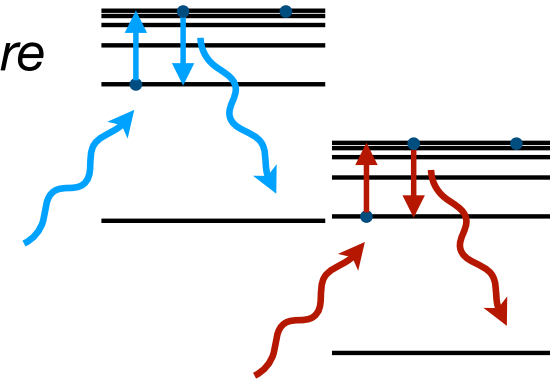


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Thermal (Doppler) broadening

$$\Delta\lambda \approx \frac{2\lambda}{c} \sqrt{\frac{2kT}{m}}$$

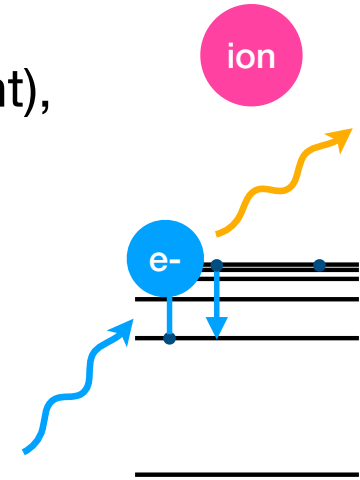
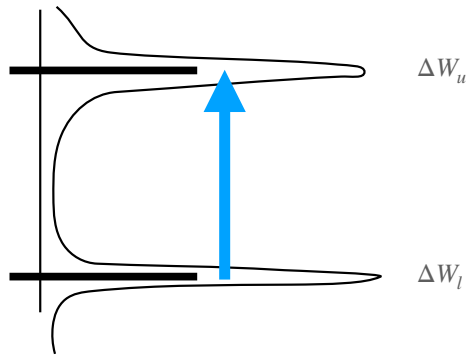
- For $H\alpha$ on (above?) the Sun, we expect just the *temperature* to cause $\Delta\lambda \approx 0.04\text{nm}$
 - MUCH LARGER than Natural Broadening...
- Other velocity motions can cause Doppler broadening i.e. not explicitly *thermal* behavior
- e.g. microturbulence, especially due to convective motions of gas



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Pressure broadening

- Collisional interaction between atoms (of the same type or different), ions, e-... even molecules in some cases.
- These interactions can blur the locations of the energy levels
- Again, due to Heisenberg, this results in line broadening



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Pressure broadening

- Collisions more frequent when pressure (and density) is high in the gas
- If we use our intuition from natural broadening, where Δt is now the typical time between collisions $FWHM = \frac{\lambda^2}{\pi c \Delta t}$
- Assume a typical velocity from the thermal motion (i.e. Doppler broadening)
- These combine to give a useful estimate:

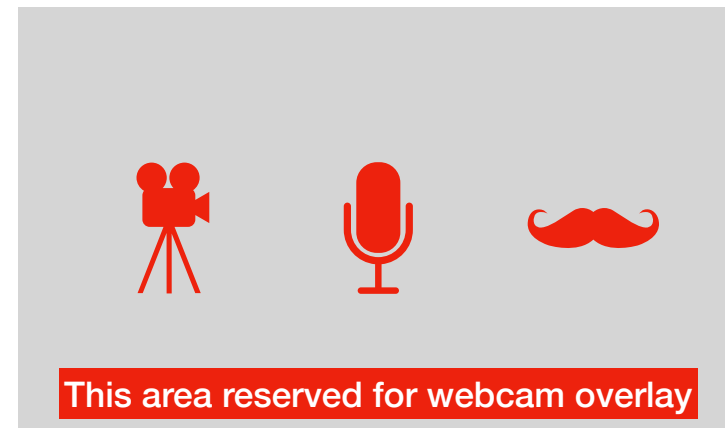
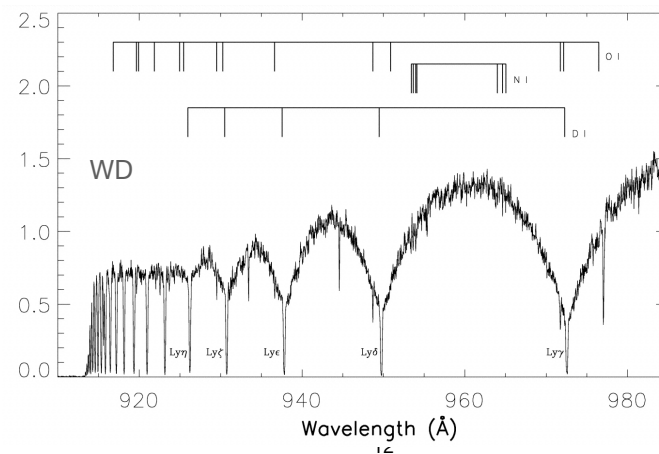
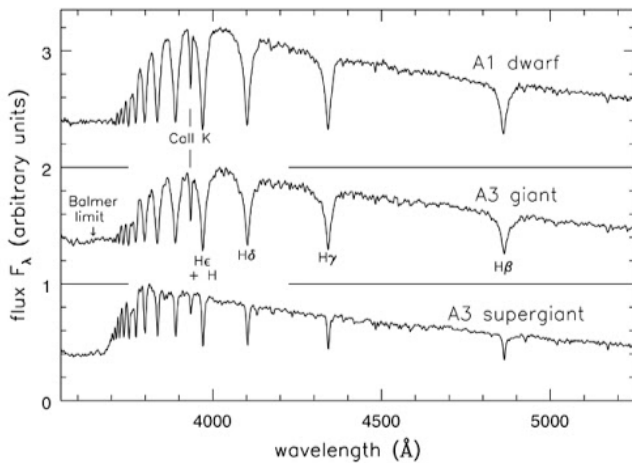
$$\Delta\lambda \approx \frac{\lambda^2 n \sigma}{\pi c} \sqrt{\frac{2kT}{m}}$$



Pressure broadening

$$\Delta\lambda \approx \frac{\lambda^2 n\sigma}{\pi c} \sqrt{\frac{2kT}{m}}$$

- Line width due to temperature, but also density of material!
- Thus Pressure broadening is the indicator of surface gravity (mean density)
- For dwarf stars, this is often small (e.g. for $H\alpha$), but can be VERY large for high surface gravity!



Pressure broadening

$$\Delta\lambda \approx \frac{\lambda^2 n\sigma}{\pi c} \sqrt{\frac{2kT}{m}}$$

- Various physics creating these collisions:
 - **Linear Stark Effect** (mostly for H lines, impacting Protons & e-)
 - **Quadratic Stark** (most lines in hot stars, impacting ions & e-)
 - **van der Waals** (most lines in cool stars, impacting neutral H)
- Can be VERY broad, esp. for strong dipoles (e.g. H)

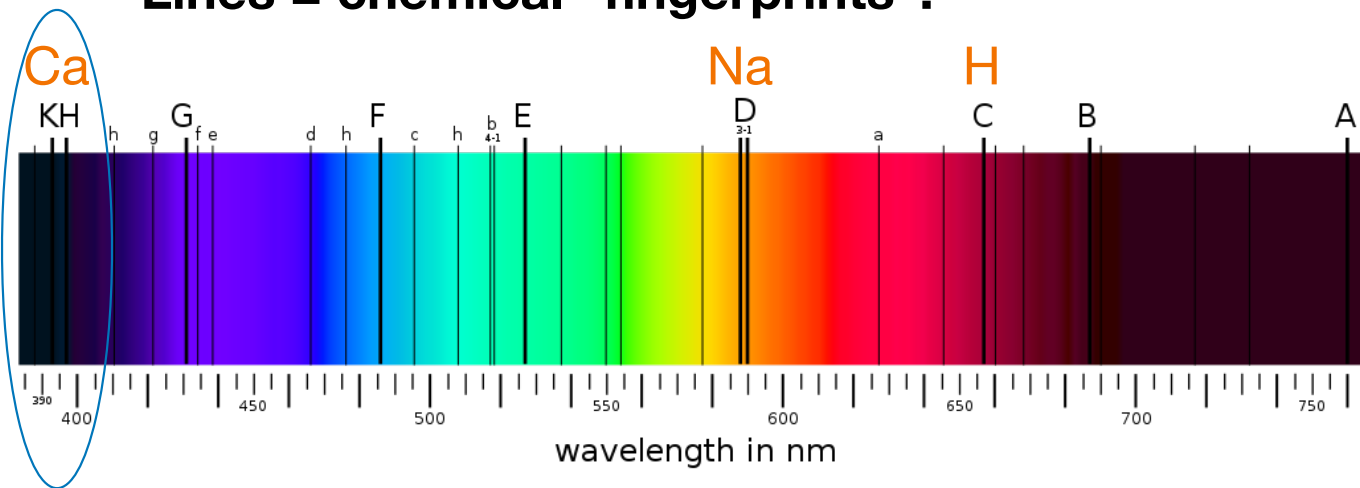
STARK EFFECT



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Fraunhofer lines

- Cataloged in solar spectrum by Fraunhofer in 1814
- Seen in many other stars
- Kirchhoff & Bunsen noticed these == emission line from burning! (1859)
Lines = chemical “fingerprints”!

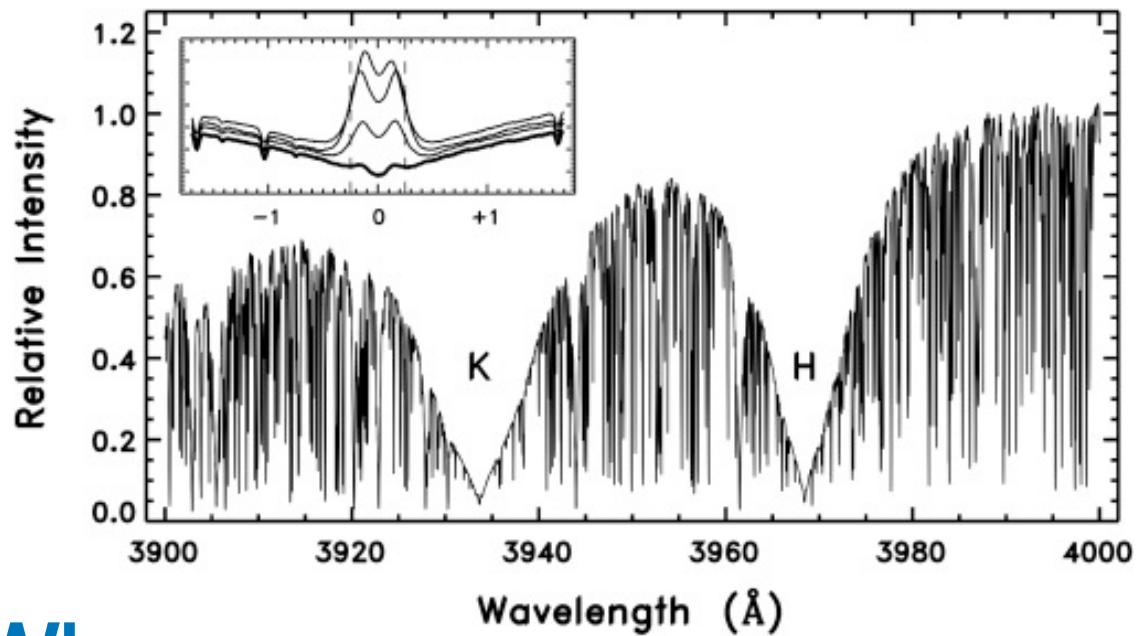


https://en.wikipedia.org/wiki/Fraunhofer_lines



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Ca II (or Ca+) “HK”



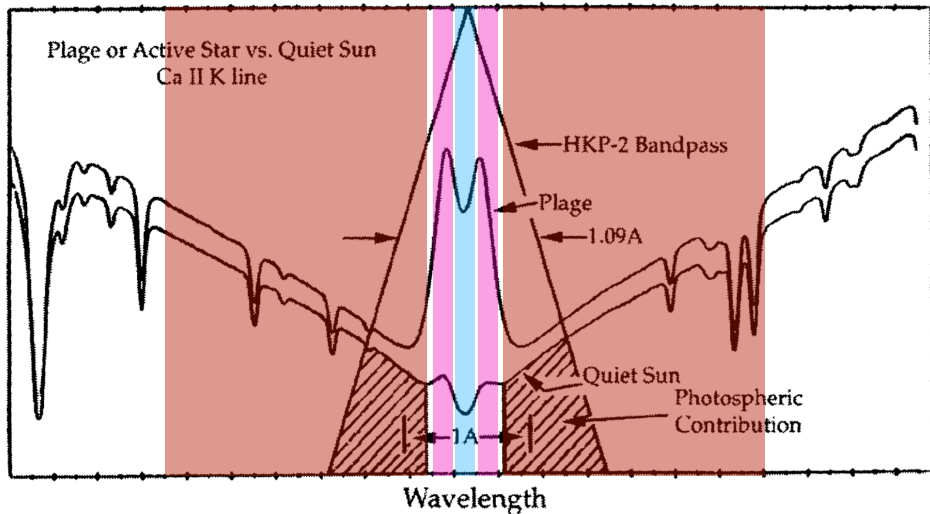
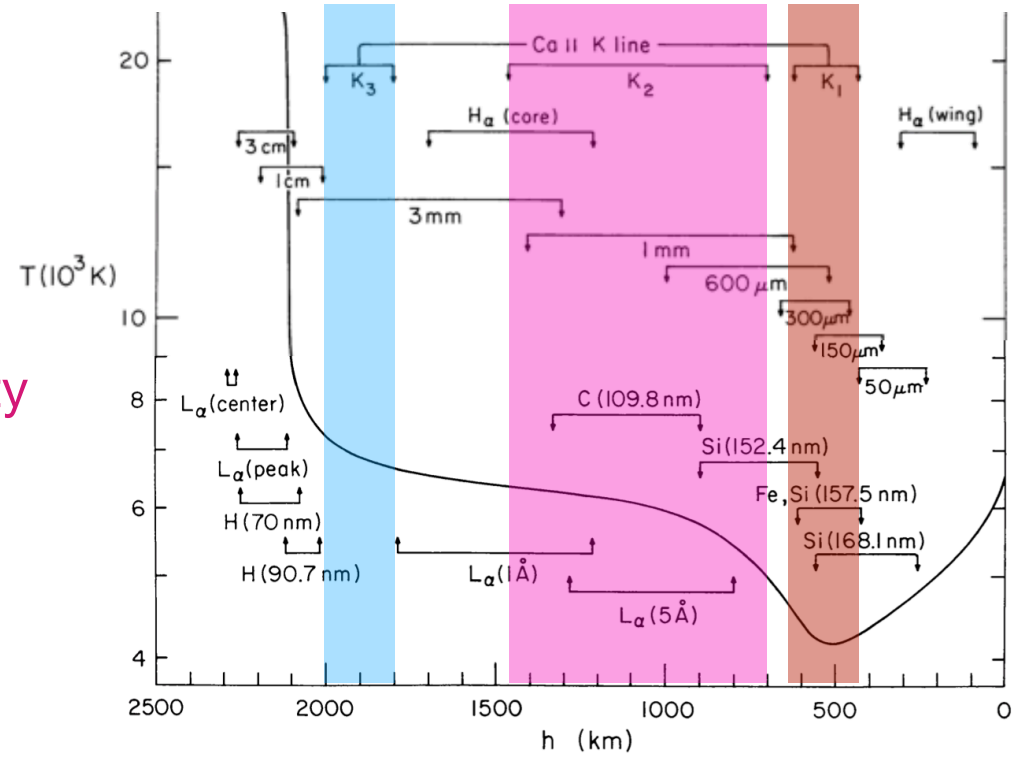
Whoa...



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Ca II (or Ca+) “HK”

Important tracer of chromospheric B activity

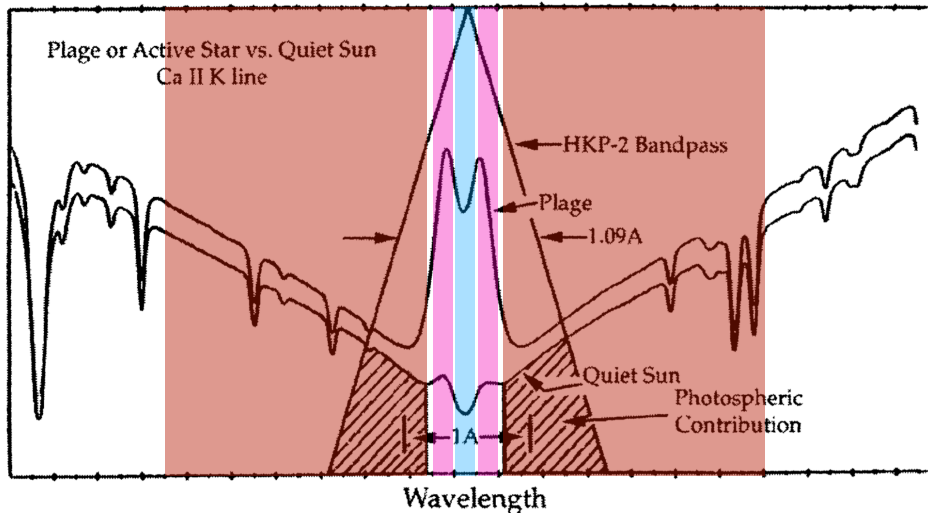
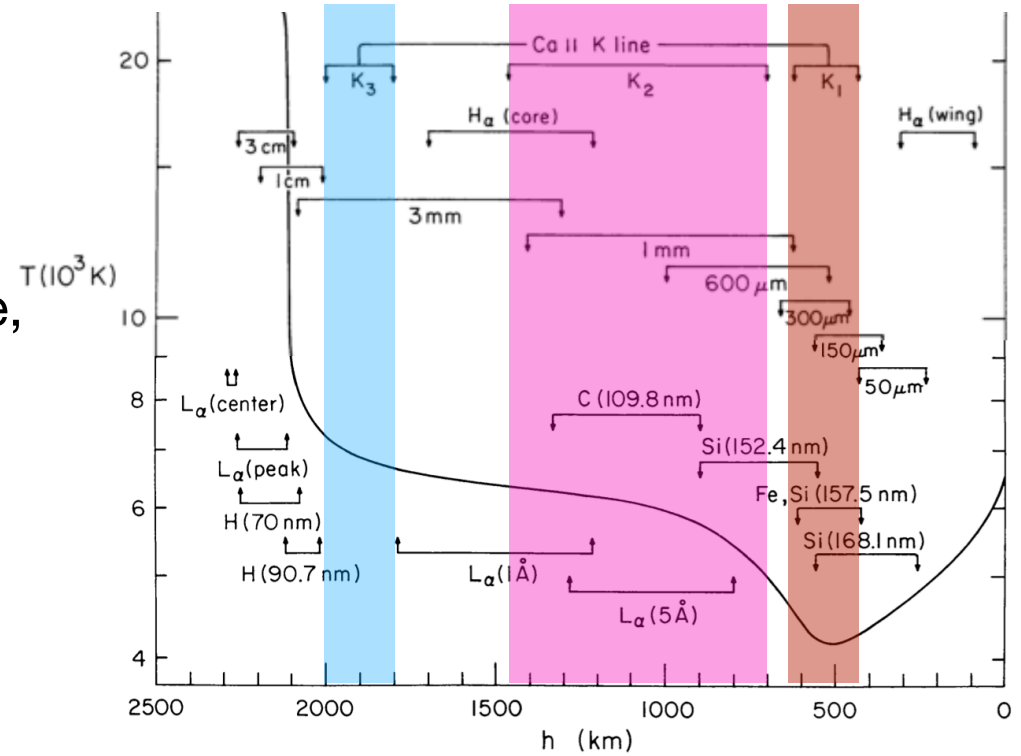


Duncan+1991, Baliunas+1998


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Ca II (or Ca+) “HK”

- **Wings** formed at photosphere surface, driven by scattering (super broad Lorentzian profile)



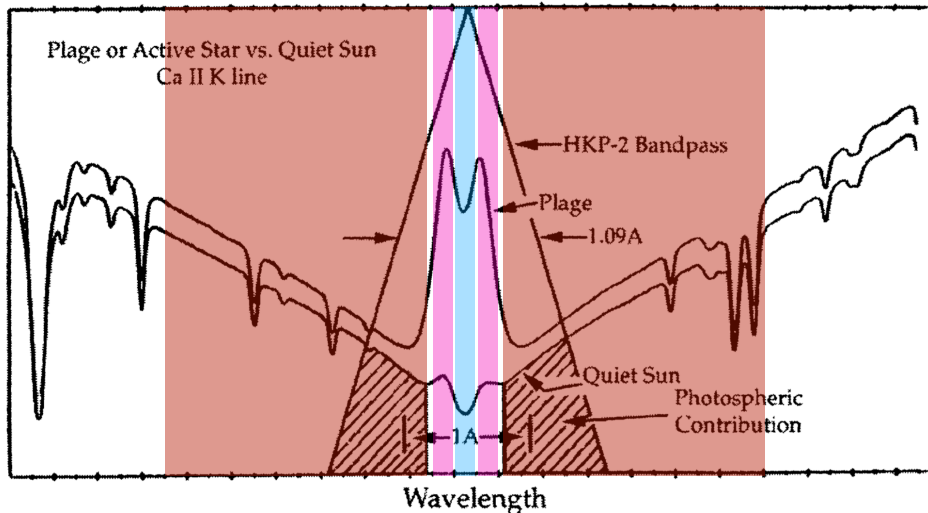
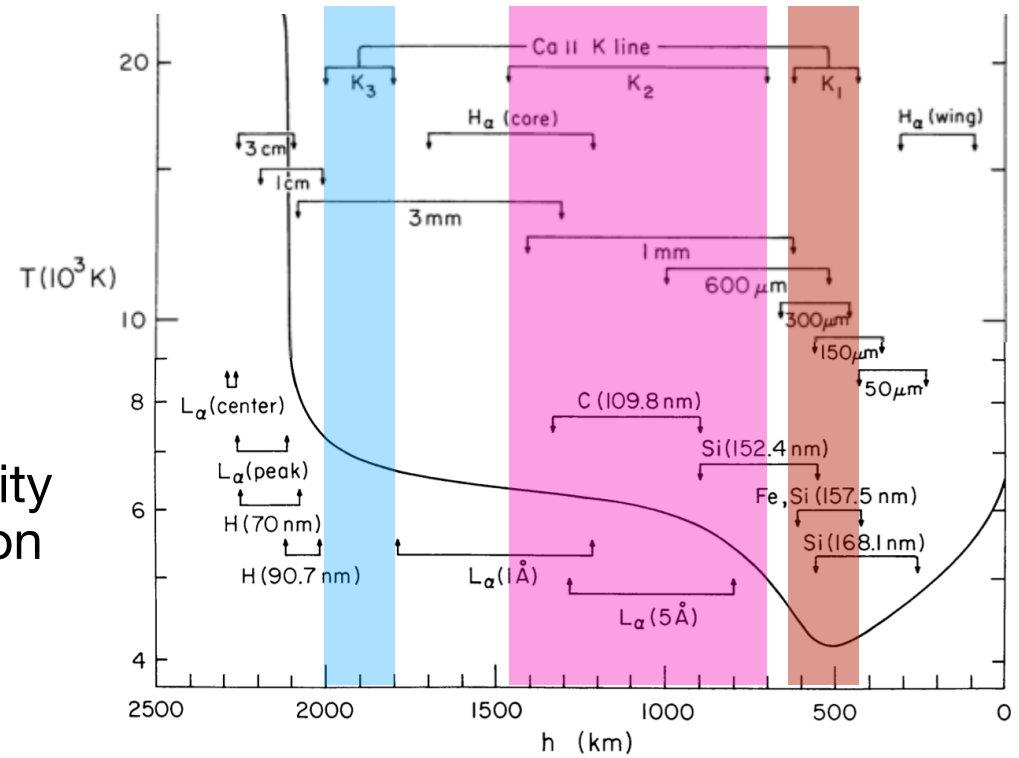
Duncan+1991, Baliunas+1998




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Ca II (or Ca+) “HK”

- **Peaks** due to increased temperature in chromosphere (like $H\alpha$)
- **Dip** due to scattering, increases opacity again right before the Transition Region



Duncan+1991, Baliunas+1998

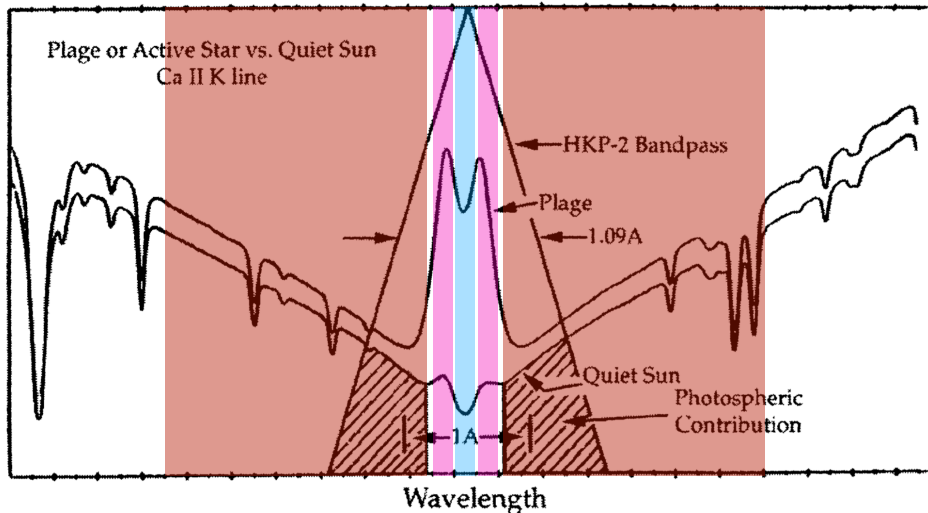
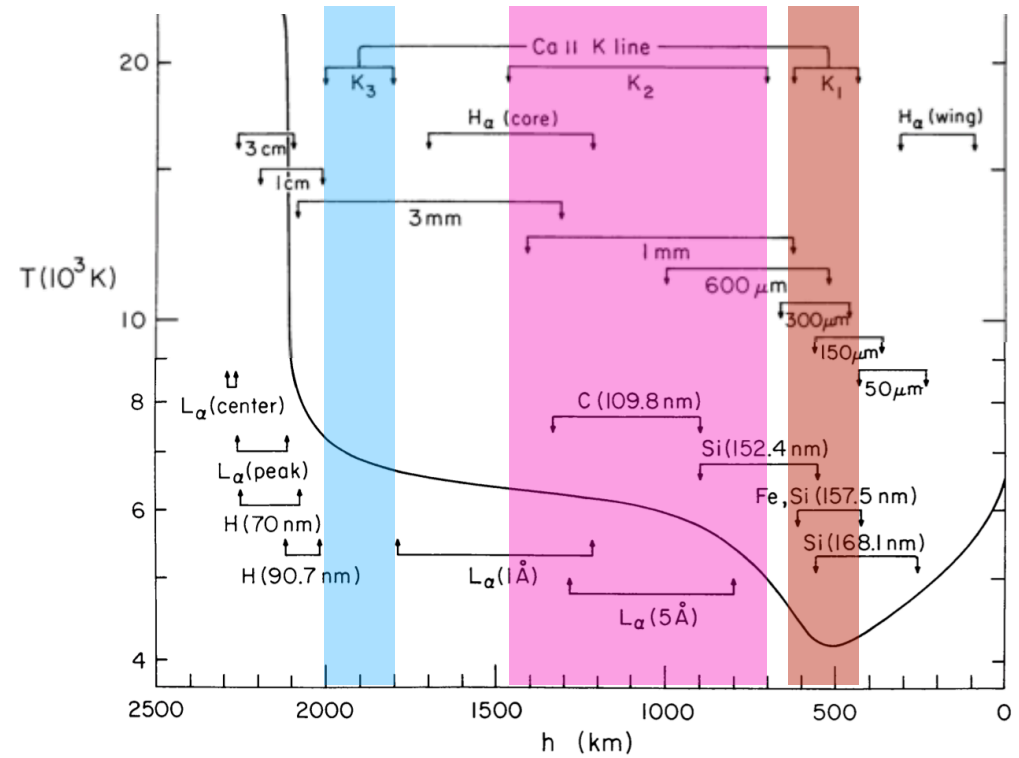


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Ca II (or Ca+) “HK”

- Interestingly, the dip can be offset from line center, due to motions of gas (Doppler shift) in the upper chromosphere

Björger+2018



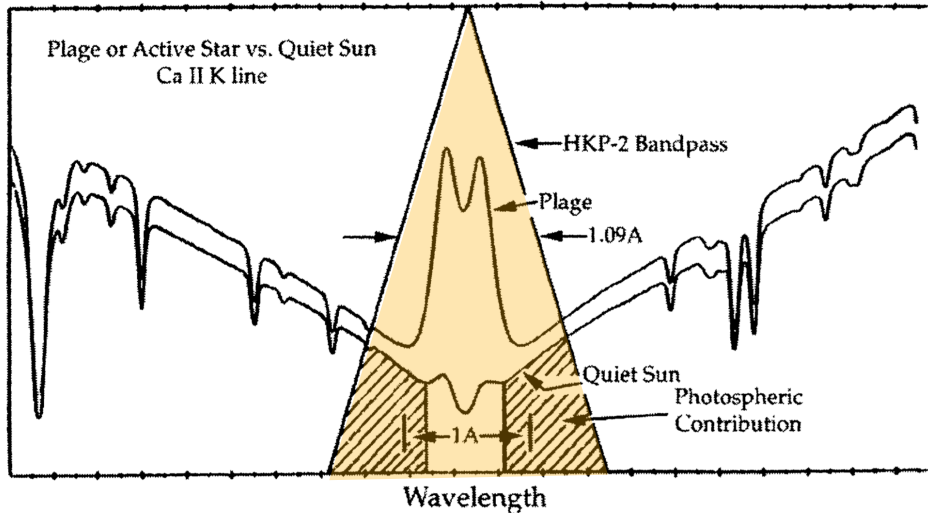
Duncan+1991, Baliunas+1998



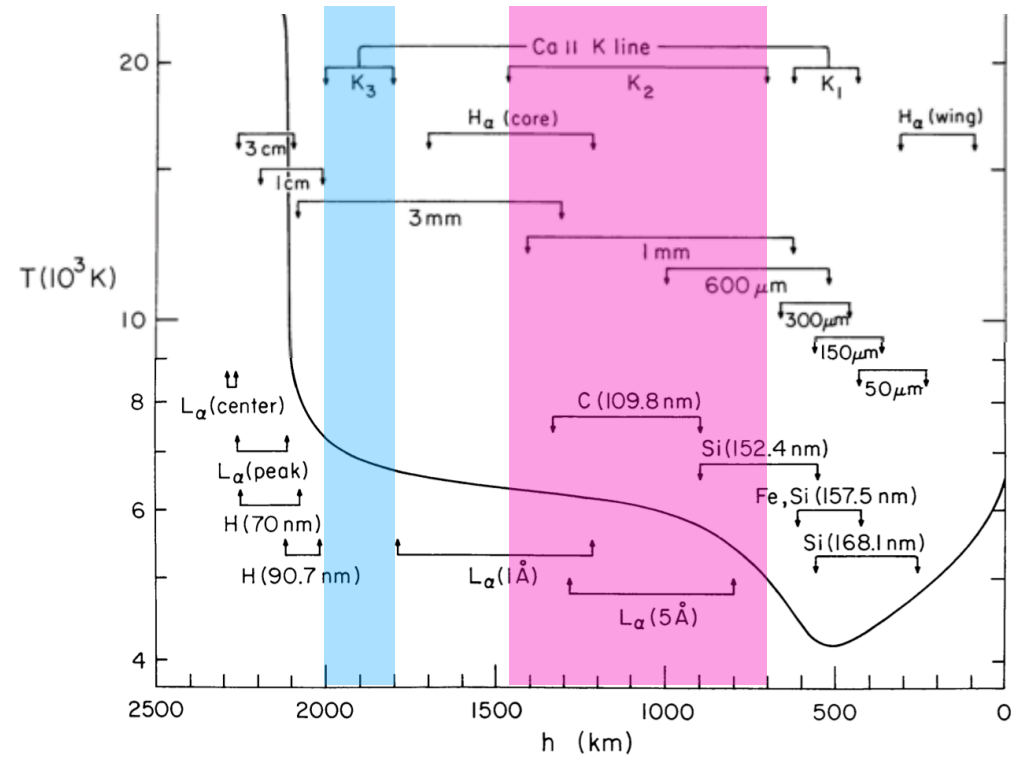
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Ca II (or Ca+) “HK”

- The core is the most “interesting” part historically
- Strongly dependent on **B** heating of the chromosphere!



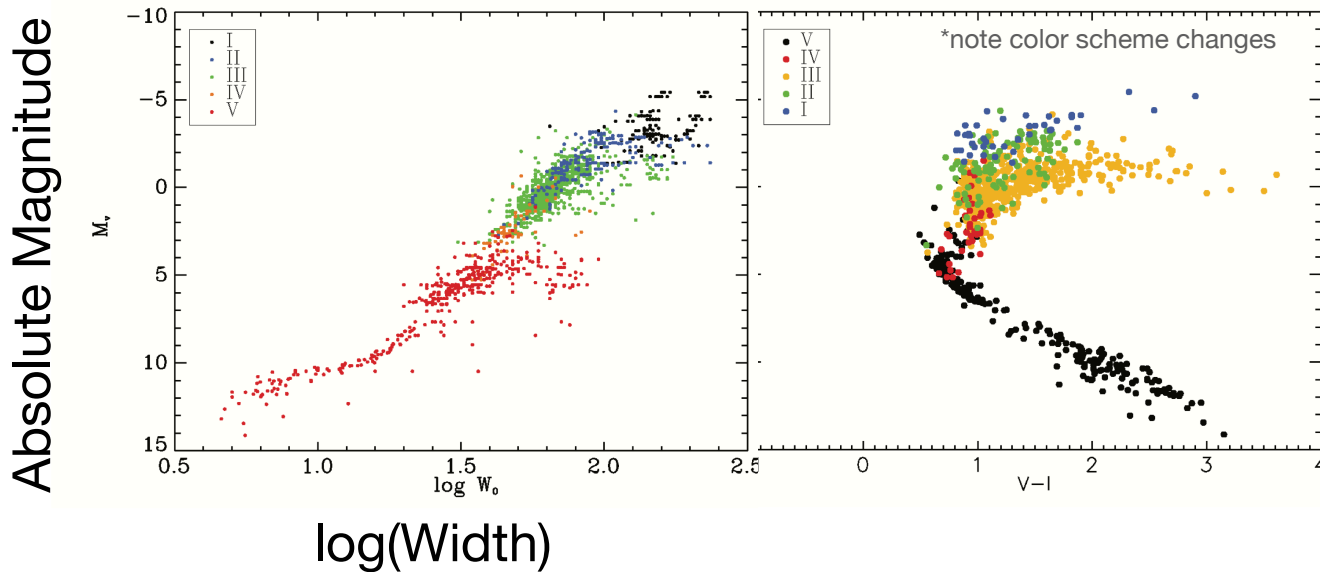
Duncan+1991, Baliunas+1998



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Wilson-Bappu Effect

- Empirical connection between width of Ca II line core and a star's *luminosity*



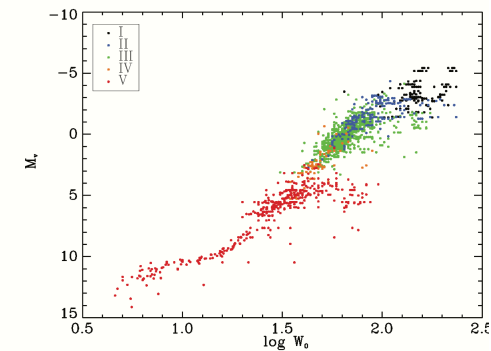
Gomez & Wallerstein (2011)



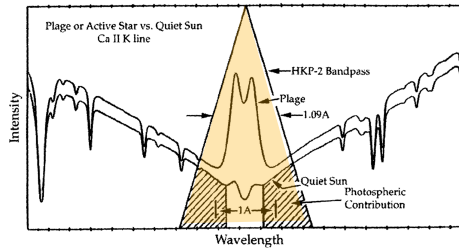
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Wilson-Bappu Effect

- Empirical connection between width of Ca II line core and a star's *luminosity*
- Since Ca II lines can be very broad, can be easier way to estimate luminosity (and thus distance) to a star...
- Ca II line definition varies from author to author works best for dwarfs with chromospheres
- Sensitive to both gravity effects AND chromospheric activity...

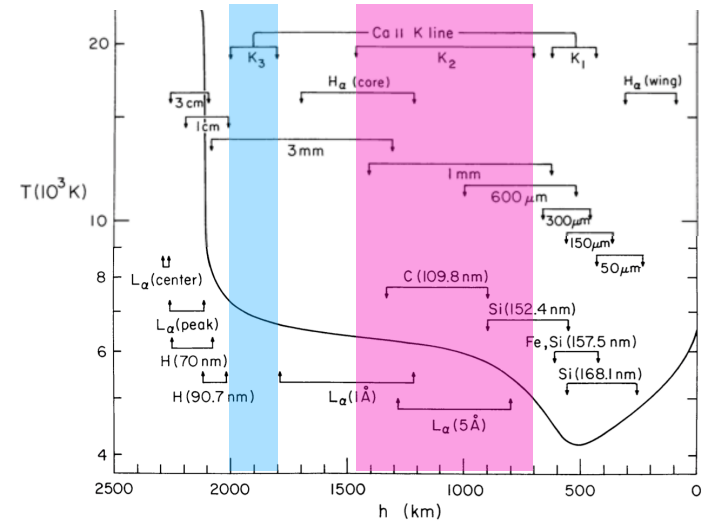


Ca II HK



Duncan+1991, Baliunas+1998

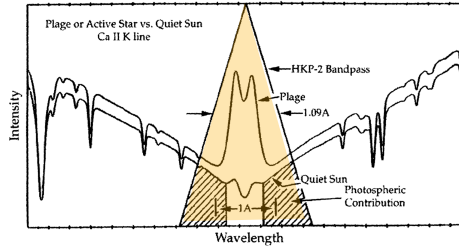
- Strongly dependent on **B** heating of the chromosphere!
- This means chromospheric heating changes if the total **B** strength changes.
- Ca II HK (and $H\alpha$) the most widely used indicators of total surface **B** field e.g. see [Hall \(2008\)](#)
- **Activity cycles... a rich history!**



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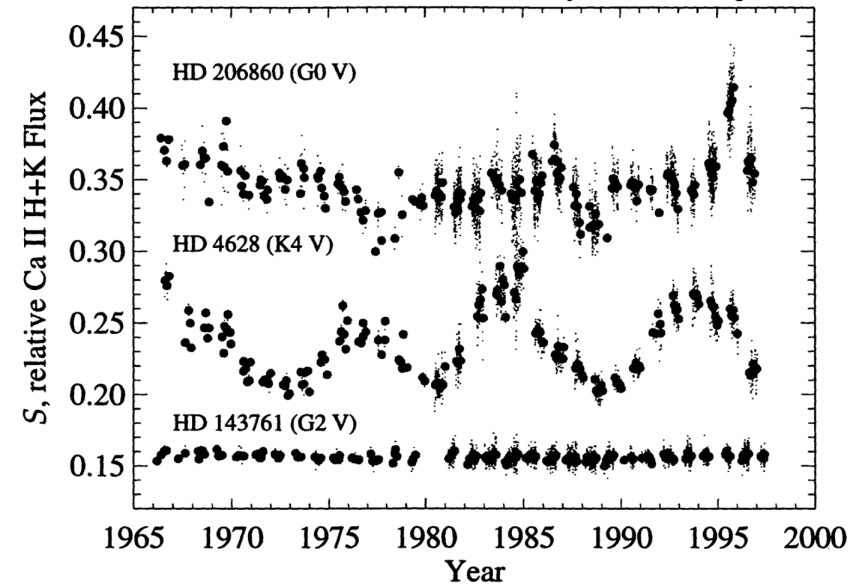
Ca II HK

- Activity cycles... a rich history!

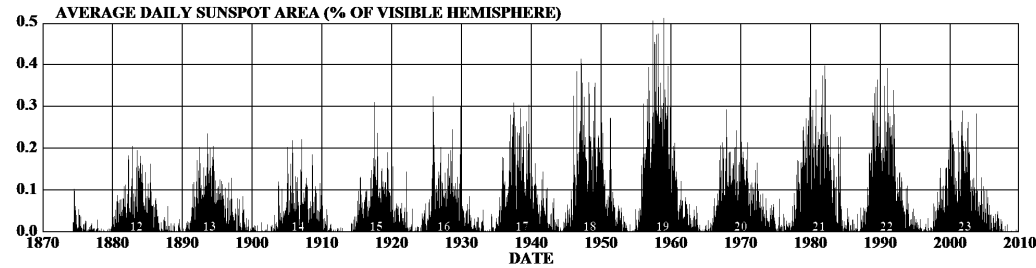
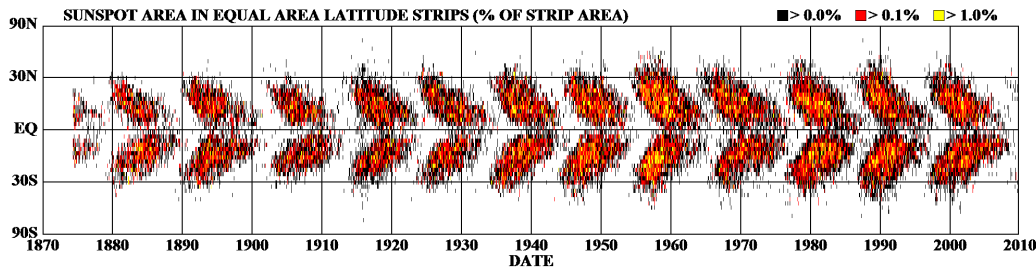


Duncan+1991, Baliunas+1998

Mount Wilson Observatory - HK Project



DAILY SUNSPOT AREA AVERAGED OVER INDIVIDUAL SOLAR ROTATIONS

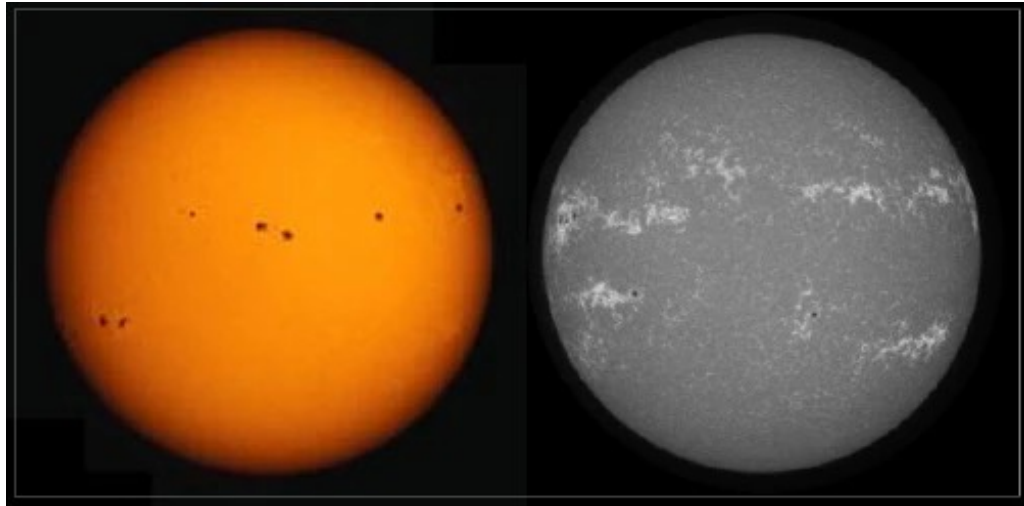


<http://solarscience.msfc.nasa.gov/>

HATHAWAY/NASA/MSFC 2009/11

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Ca II HK



Visible light
(broadband)

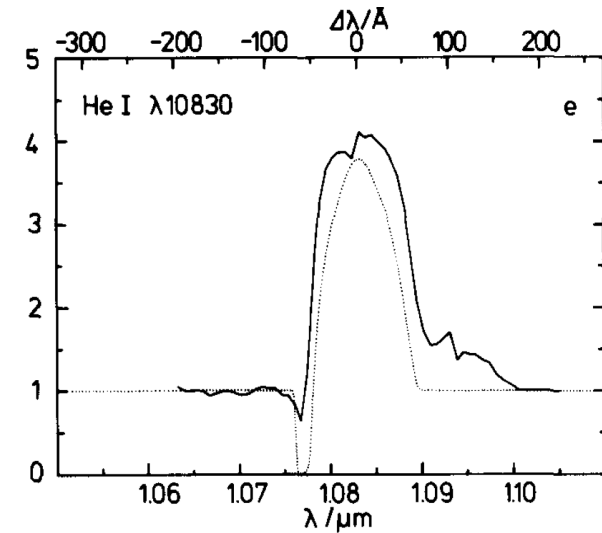
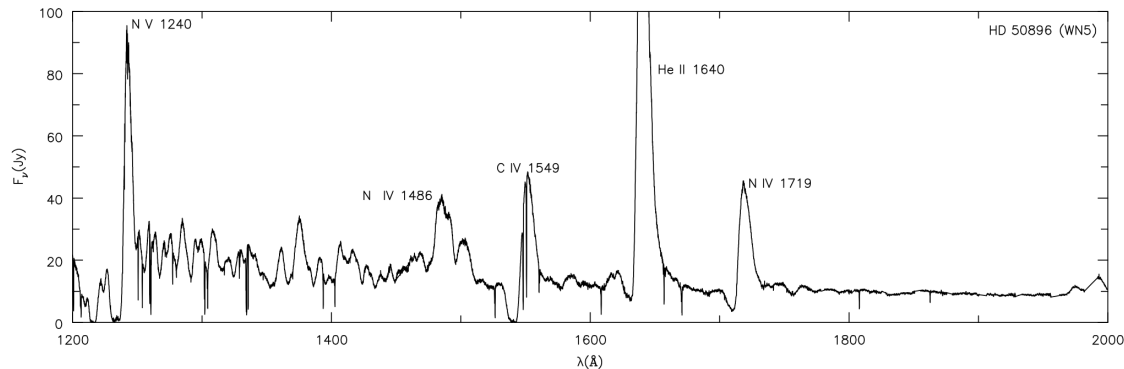
Ca II K filter



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Emission lines in Wolf Rayet stars?

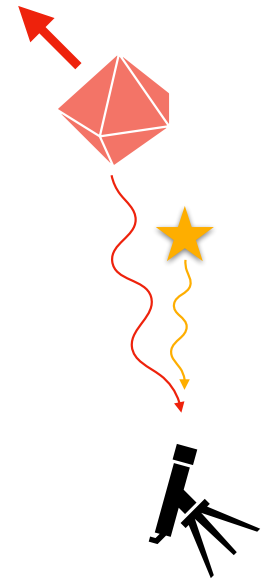
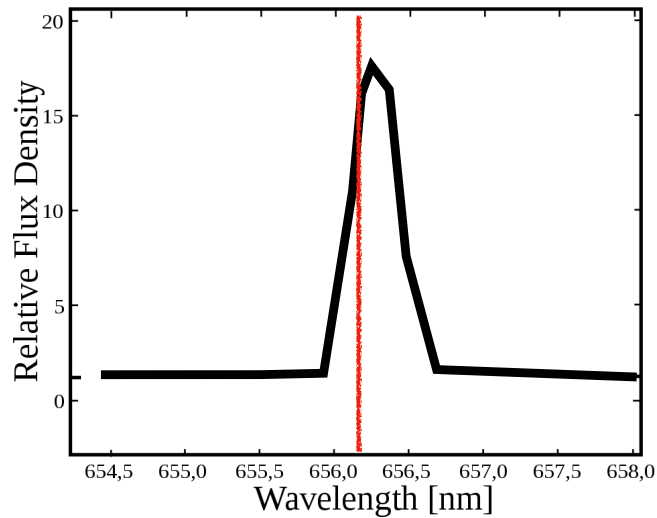
- Line profiles are REALLY interesting
- Very broad, very Gaussian, but not totally symmetric...



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Emission lines from outflows

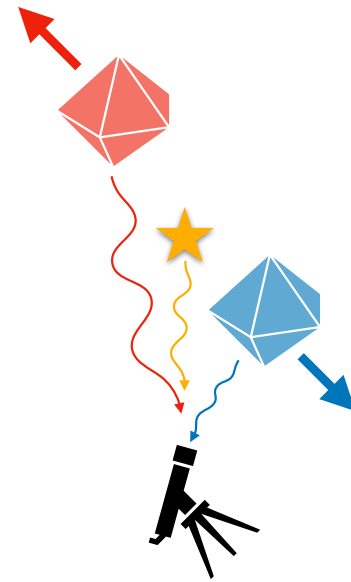
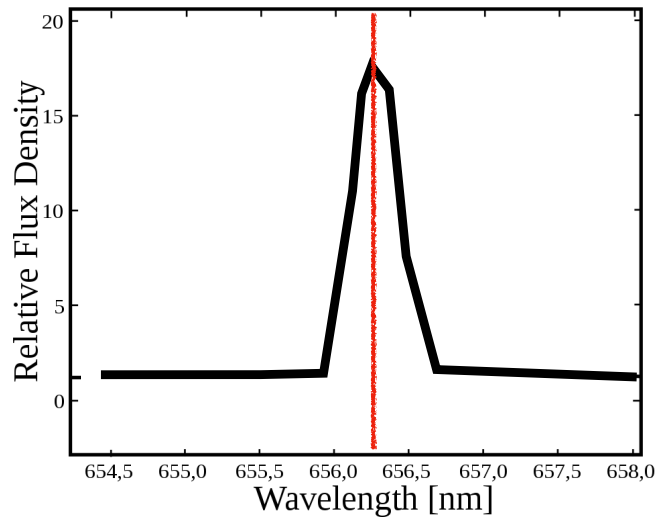
Red-shifted line: *motion away*



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Emission lines from outflows

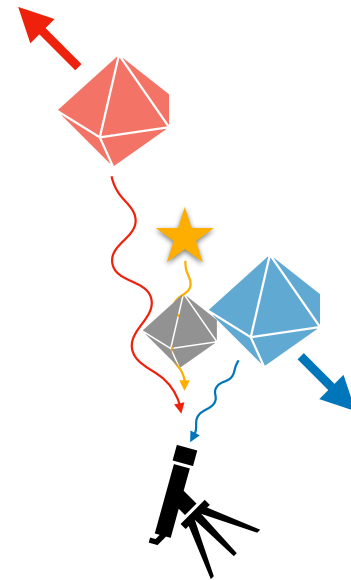
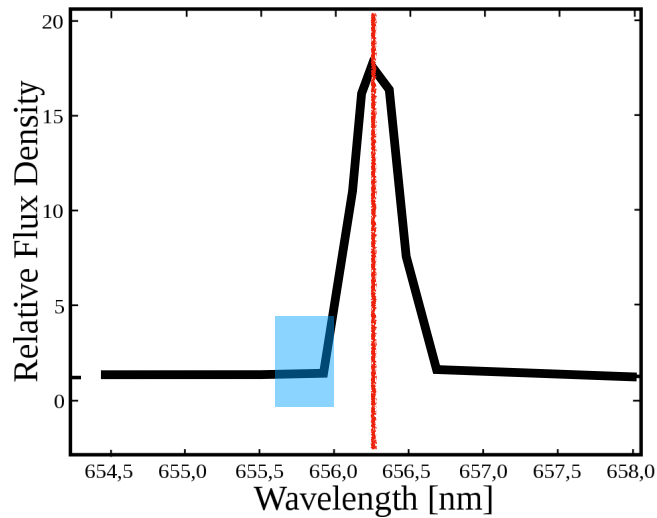
Broadened line: *motion all directions*



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Emission lines from outflows

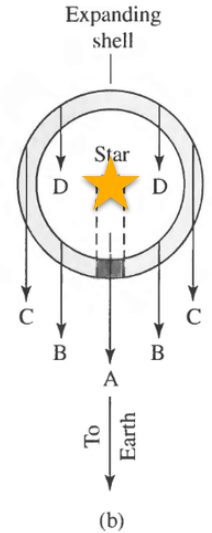
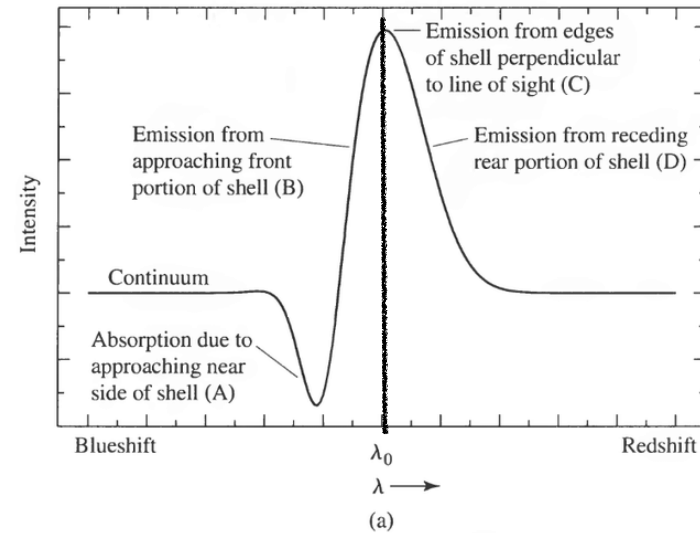
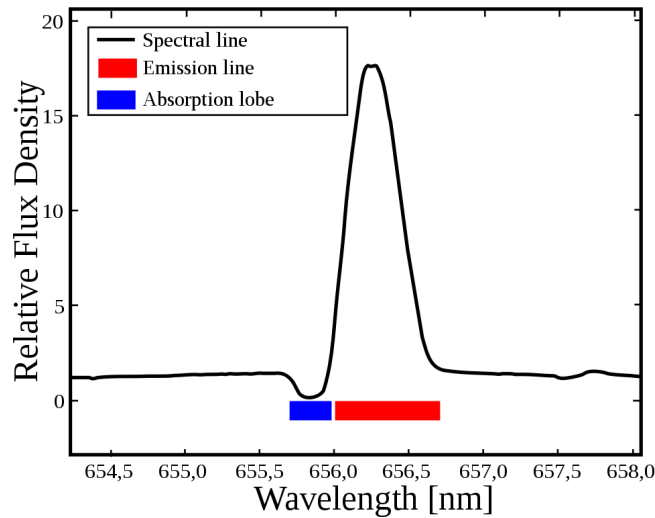
What happens when some of the outflow gets in the way of the star?



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Emission lines from outflows

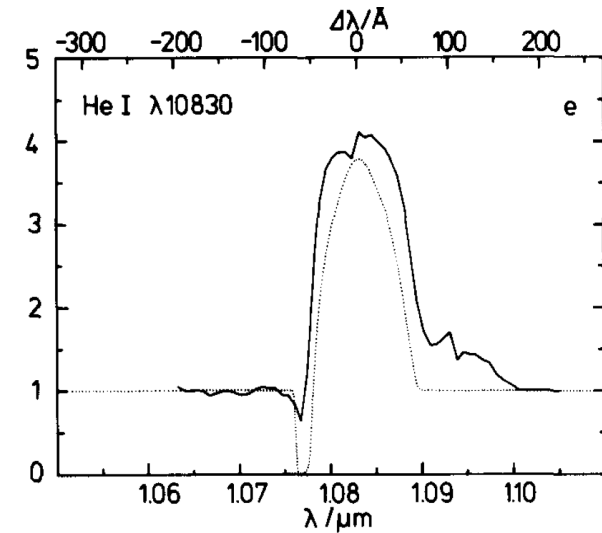
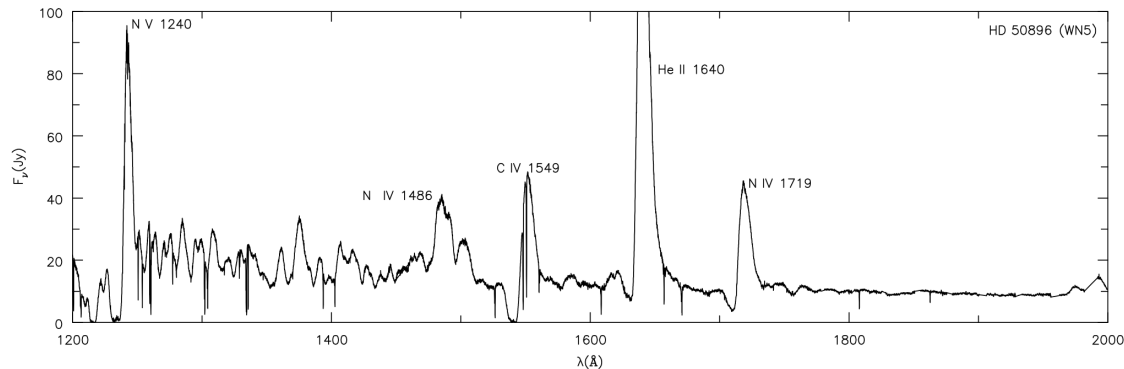
P Cygni line profile:
expanding shell of material



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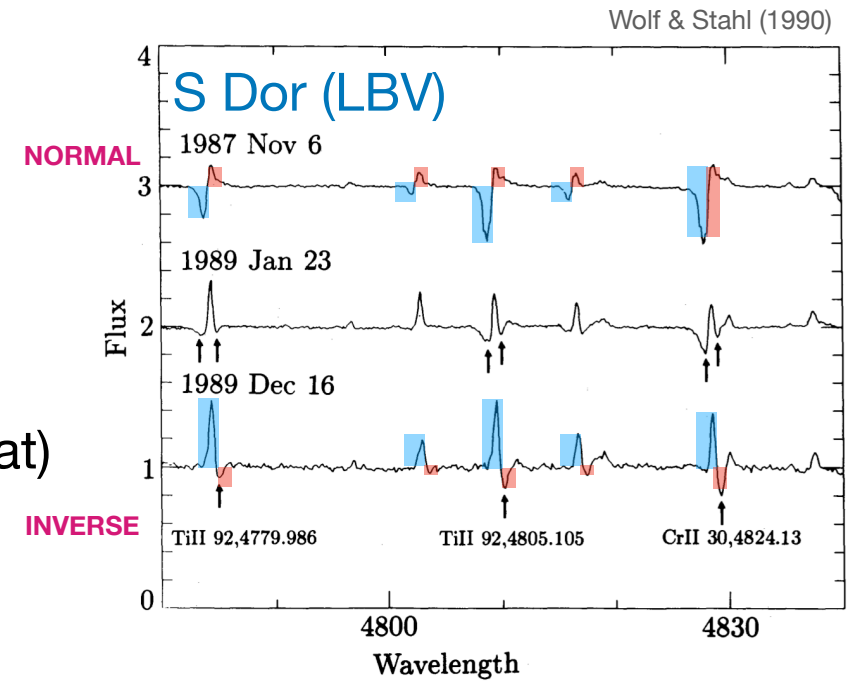
Emission lines in Wolf Rayet stars?

- Line profiles are REALLY interesting
- Very broad, very Gaussian, but not totally symmetric...



Inverse P Cygni Profiles

- If a P Cygni profile is a classical indicator of outflows... an *inverse* P Cygni = *infall*
- We DO see this... here's a really strange (neat) example of a star that shows **both**
- An indicator of *accretion!*



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Inverse P Cygni Profiles

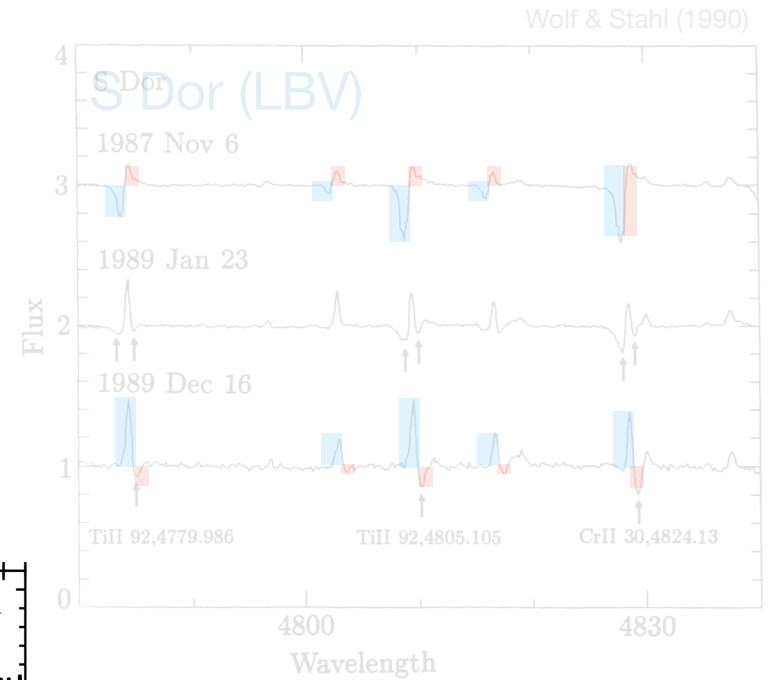
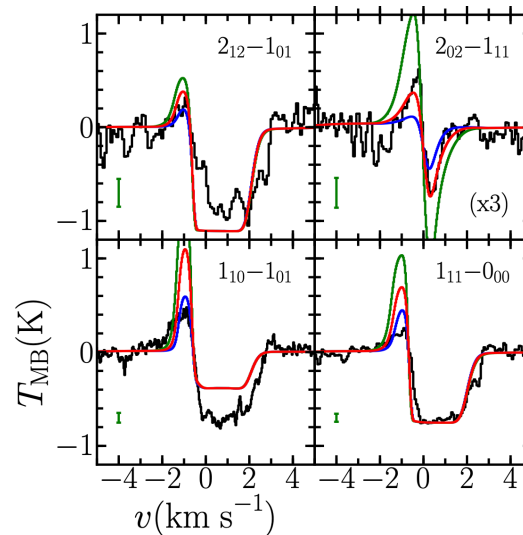
- If a P Cygni profile is a classical indicator of outflows... an *inverse* P Cygni = *infall*
- We DO see this... here's a really strange (neat) example of a star that shows **both**

- An indicator of *accretion!*

- Example of H₂O lines around protostars

- “*Waterfalls around Protostars*”, amazing paper title....

Mottram+2013



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Next time...

- Extracting stellar parameters from spectral lines
- Also point to a really good, short (<20 min) primer on line broadening by Aaron Parsons (Berkeley): <https://www.youtube.com/watch?v=wzhnF66ZomE>



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